

COLOR SELECTION SCHEME FOR DIGITAL VIDEO WATERMARKING

Cross-Reference to Related Applications

U.S. patent applications Serial No. (Zarrabizadeh 22) and Serial No. (Zarrabizadeh 23) were filed concurrently herewith.

5 Technical Field

This invention relates to the art of watermarking digital video, and more particularly, to selecting which chrominance portion should be watermarked.

Background of the Invention

Watermarking of video signals is, generally, the inclusion within the video itself
10 of additional information. This can be useful to provide an embedded identification of the source of a video, to keep track of where and for how long a video is played, and to communicate information via the video to an ancillary device. Prior art techniques for watermarking video signals typically encoded the additional information in an analog format within the video itself using the luminance of the video to carry the additional
15 information. However, the human visual system is very sensitive to the luminance signal, and so a person viewing a watermarked signal easily perceives distortion which is caused by the changes made to the video signal to convey the additional information when there is an attempt to increase the bit rate of the additional information beyond a certain point, e.g., beyond 120 bits per second. Thus, although the prior art's techniques of
20 watermarking of video signals has had some success in certain applications, such success has been limited by the extremely small bit rate that is achievable without perceivable distortion by a person viewing the video signal carrying the additional information.

In previously filed United States Patent Application Serial No. 10/342704, which is incorporated by reference as if set forth fully herein, I, along with my coinventor,
25 recognized that the human visual system is much less sensitive to chrominance than to luminance. Therefore, we developed a system for digital watermarking a video signal that inserts the additional information of the watermarking signal on the chrominance component of the video signal rather than on its luminance signal. Thus, the additional information is "impressed" upon the chrominance component of the video signal.
30 Advantageously, although there may be significant distortion of the chrominance component, especially when the additional information has higher bit rates than is achievable without perceivable distortion by the prior art, nevertheless such distortion will not be detected by the human visual system, provided it is appropriately managed.

Thus, the additional information can have a higher bit rate as compared with that achievable by the prior art, e.g., bit rates greater than 150 bits per second can be achieved. Further advantageously, the additional data can be recovered from the video signal even after the video signal watermarked with the additional data is compressed using the Motion Picture Expert Group (MPEG)-1 and MPEG-2 encoding systems.

The particular chrominance portion selected to carry the watermarking for any pixel is selected in United States Patent Application Serial No. 10/342704 by a color selection unit. The color selection unit determines the selected chrominance component as a function of the RGB and the YUV representations of the pixel using a prescribed formula. Since digital video is often transmitted only in YUV format, to use the system of United States Patent Application Serial No. 10/342704 with such YUV formatted video, it is necessary to develop therefrom the corresponding RGB formatted video. Disadvantageously, to do so requires considerable processing power. Furthermore, although it is very good, it was later discovered that the mathematical model underlying the formula employed in the selection process of United States Patent Application Serial No. 10/3427 does not necessarily always produce flicker-free results.

Summary of the Invention

In accordance with the principles of the invention, the process of determining the chrominance portion to be watermarked may be improved by employing a perception-based table that indicates for various pixels which of the chrominance portions, if any, should be selected for watermarking. In accordance with an aspect of the invention, only values for Y, U, and V of a pixel may be required to access the table and determine which chrominance portion should be selected. Advantageously, when the digital video is in YUV format, the use of R, G, and B is not required to select the chrominance portion, thereby reducing significantly the necessary processing power. In accordance with another aspect of the invention, the table may be represented such that it may be accessed using only R, G, and B values, so that there is no need to convert a source video in RGB format to YUV format in order to perform color selection.

In one embodiment of the invention, the table is accessed by supplying Y, U, and V values, which may be decimated and/or quantized, and retrieving from the table an indication of whether U or V should be selected. In accordance with yet another aspect of the invention, the table may be modified so that it may indicate which of U or V should be selected, or that neither should be selected, e.g., when the color of the pixel is dark blue and/or dark purple, indicating that this pixel should not be watermarked at all.

In accordance with another aspect of the invention, a mixed-mode of processing may be employed using the table and some processing. Advantageously, the table may be simplified, e.g., reduced by half its size, because a large section of the table may be replaced by a simple test on the pixel values, e.g., $U < 128$, to determine the selected chrominance portion.

Advantageously, the table may be changed on the fly without changing the underlying process, e.g., computer code, employed in the selection process.

Brief Description of the Drawing

In the drawing:

FIG. 1 shows an exemplary transmitter for digital watermarking a video signal, in accordance with the principles of the invention;

FIG. 2 shows an exemplary receiver for recovering the additional data of a video signal containing digital watermarking on the chrominance signal thereof, in accordance with the principles of the invention;

FIGs. 3A and 3B, when connected together as shown in FIG. 3, show an exemplary process for use in watermarking one of the chrominance portions with additional data, in accordance with the principles of the invention;

FIGs. 4A and 4B, when connected together as shown in FIG. 4, show an exemplary process for extracting the additional information from a digitally watermarked video signal in which the additional information that constitutes the watermarking signal within the video signal has been impressed upon the chrominance component, in accordance with the principles of the invention;

FIG. 5 shows an example of several safe ranges where the desired bit position is the third least significant bit;

FIG. 6 shows an exemplary process for determining which particular chrominance portion is more suitable, and so should be selected, to contain the watermarking information for a pixel, in accordance with the principles of the invention;

FIG. 7 shows a cutaway view of a portion of an exemplary divided colorspace;

FIG. 8 shows another exemplary process by which the particular chrominance portion is selected to contain the watermarking information for a pixel, in accordance with the principles of the invention;

FIG. 9 shows an exemplary transmitter arranged in accordance with the principles of the invention, in which flickering may be reduced by replicating the data to be impressed, at least once, and preferably two or more times, prior to its being impressed upon the average value of a chrominance portion of a block; and

FIG. 10 shows an exemplary embodiment of a receiver arranged in accordance with the principles of the invention for use in receiving a watermarked video signal such as that produced by the transmitter of FIG. 9.

Detailed Description

5 The following merely illustrates the principles of the invention. It will thus be appreciated that those skilled in the art will be able to devise various arrangements which, although not explicitly described or shown herein, embody the principles of the invention and are included within its spirit and scope. Furthermore, all examples and conditional language recited herein are principally intended expressly to be only for pedagogical
10 purposes to aid the reader in understanding the principles of the invention and the concepts contributed by the inventor(s) to furthering the art, and are to be construed as being without limitation to such specifically recited examples and conditions. Moreover, all statements herein reciting principles, aspects, and embodiments of the invention, as well as specific examples thereof, are intended to encompass both structural and
15 functional equivalents thereof. Additionally, it is intended that such equivalents include both currently known equivalents as well as equivalents developed in the future, i.e., any elements developed that perform the same function, regardless of structure.

 Thus, for example, it will be appreciated by those skilled in the art that any block diagrams herein represent conceptual views of illustrative circuitry embodying the
20 principles of the invention. Similarly, it will be appreciated that any flow charts, flow diagrams, state transition diagrams, pseudocode, and the like represent various processes which may be substantially represented in computer readable medium and so executed by a computer or processor, whether or not such computer or processor is explicitly shown.

 The functions of the various elements shown in the FIGs., including any
25 functional blocks labeled as “processors”, may be provided through the use of dedicated hardware as well as hardware capable of executing software in association with appropriate software. When provided by a processor, the functions may be provided by a single dedicated processor, by a single shared processor, or by a plurality of individual processors, some of which may be shared. Moreover, explicit use of the term “processor”
30 or “controller” should not be construed to refer exclusively to hardware capable of executing software, and may implicitly include, without limitation, digital signal processor (DSP) hardware, network processor, application specific integrated circuit (ASIC), field programmable gate array (FPGA), read-only memory (ROM) for storing software, random access memory (RAM), and non-volatile storage. Other hardware,
35 conventional and/or custom, may also be included. Similarly, any switches shown in the

FIGS. are conceptual only. Their function may be carried out through the operation of program logic, through dedicated logic, through the interaction of program control and dedicated logic, or even manually, the particular technique being selectable by the implementer as more specifically understood from the context.

In the claims hereof any element expressed as a means for performing a specified function is intended to encompass any way of performing that function including, for example, a) a combination of circuit elements which performs that function or b) software in any form, including, therefore, firmware, microcode or the like, combined with appropriate circuitry for executing that software to perform the function. The invention as defined by such claims resides in the fact that the functionalities provided by the various recited means are combined and brought together in the manner which the claims call for. Applicant thus regards any means which can provide those functionalities as equivalent as those shown herein.

Software modules, or simply modules which are implied to be software, may be represented herein as any combination of flowchart elements or other elements indicating performance of process steps and/or textual description. Such modules may be executed by hardware which is expressly or implicitly shown.

Unless otherwise explicitly specified herein, the drawings are not drawn to scale.

In the description, identically numbered components within different ones of the FIGs. refer to the same components.

FIG. 1 shows exemplary transmitter 101 for digital watermarking a video signal in accordance with the principles of the invention, by having one or more bits of watermark data carried via an average value of the chrominance component of each of various blocks of the video signal, on up to a per-frame basis.

Shown in FIG. 1 are a) YUV demultiplexer (demux) and decimator 103, b) color selection 105, c) double-pole, double-throw switch 109, d) texture masking unit 111, e) multiplier 113, f) adder 115, g) multiplexer (mux) 117, h) bit mapper 123, and i) summer 133. Also shown in FIG. 1 are optional j) channel encoder 119, and k) block interleaver 121.

YUV demultiplexer and decimator 103 receives a video signal to be watermarked, i.e., to have additional information added thereto. YUV demultiplexer and decimator 103 may work with digital video, e.g., video formatted according to the Serial Digital Interface (SDI) standard. As will be recognized by those of ordinary skill in the art, any video signal not initially in an appropriate digital format may be converted thereto using conventional techniques.

YUV demultiplexer and decimator 103 demultiplexes the luminance (Y) component of the video and its chrominance component. The chrominance component of the video signal has two portions U and V, where U is the differential blue portion and V is the differential red portion.

5 Much of the processing to embed the additional data on the chrominance component is, preferably, performed with a special decimated video format in which for each original 2x2 luminance block of video, had the original block been in 4-4-4 representation, there remains only one Y, one U, and one V value. To this end, in the event the input video signal is actually in the so-called 4-4-4 format, the image is
10 appropriately decimated by YUV demultiplexer and decimator 103 so that for each original 2x2 luminance block there is one Y, one U, and one V value. Similarly, in the event the input video signal is in the so-called "4-2-2" format, i.e., the luminance is full resolution while the chrominance portions are a) full resolution vertically only and b) half resolution horizontally, YUV demultiplexer and decimator 103 decimates the luminance
15 component horizontally and vertically as well as decimates each chrominance portion only vertically. Likewise, in the event the input video signal is in the so-called 4-2-0 format, i.e., the luminance component is full resolution while the chrominance portions are each only half resolution both vertically and horizontally, the luminance component of the image is decimated by YUV demultiplexer and decimator 103 so that for each
20 original 2x2 luminance block had the original block been in 4-4-4 representation there remains only one Y, one U, and one V value.

The preferred decimated video format may be supplied as an output to color selection 105. Thus, preferably, regardless of the format of the input video signal, further processing by the system preferably may be based on the decimated video signal such that
25 for every 2x2 block of full resolution luminance pixels of the original input video signal there is one Y, one U, and one V value. Those of ordinary skill in the art will be able to develop their own methods, should they choose to do so, of developing one Y, one U, and one V value for every 2x2 block of luminance pixels.

In order to know the format of the original video, a) an operator may indicate to
30 YUV demultiplexer and decimator 103 the particular format of the video supplied to transmitter 101, b) the format of the video may be detected directly from the video using conventional techniques, or c) the information may be supplied from a higher layer processor which is supplying the input video signal.

YUV demultiplexer and decimator 103 may also supply a second set of YUV
35 outputs in the full format of the original input video signal to double-pole, double-throw switch 109.

Color selection 105 determines, for any particular pixel, on which portion of the chrominance component, i.e., on the U portion or the V portion, a change in value, if necessary, may be better accommodated without introducing a visible artifact. In one embodiment of the invention, color selection 105 is based upon a look-up table as described further hereinbelow. Alternatively, it may be based all or in part, on various computations, such as in prior United States Patent Application Serial No. 10/342,704.

The output of color selection 105 is also used to control the position of double-pole, double-throw switch 109. More specifically, the output of color selection 105 is set so that double-pole, double-throw switch 109 1) supplies, to adder 115, the portion of the chrominance component that has been selected to carry the watermark data; and 2) supplies, to YUV multiplexer 117, the portion of the chrominance component that was not selected. The output of color selection 105 is also supplied to multiplexer 117 and to bit mapper 123 for use as described hereinbelow.

Texture masking unit 111 analyzes the texture of the luminance area around each pixel in the decimated format supplied as output by YUV demux and decimator 103 to determine the maximum change in value that can be accommodated by that pixel without introducing visible artifacts, and supplies as an output a weight indicative thereof. The weight value may be coded, e.g., taking integral values from 1 to 5. Other values may be used, e.g., experiments have indicated that a value of up to 20 may be used in busy areas without visual degradation. The weight is supplied to multiplier 113. Texture masking unit 111 may put out a smaller value than the maximum distortion that can be introduced into a pixel as will be described hereinbelow.

Note that the particular values used are at least partially dependent on the number of bits used to represent each Y, U, and V value. For example, the foregoing suggested weight values of 1 to 5, and a weight of even up to 20, are for Y, U, and V being 8 bit values. Those of ordinary skill in the art will readily recognize that the values employed for 8 bits may be scaled to 10 bits by multiplying by 4, e.g., shifting the value to the left two times. Likewise, other numbers of bits used for Y, U, and V can be similarly accommodated.

Multiplier 113 multiplies the weight received from texture masking unit 111 by a value related to the information to be transmitted as part of this pixel, which is supplied by bit mapper 123. For example, the value supplied by bit mapper 123 may be -1, 0, or 1. The product produced by multiplier 113 is supplied to adder 115 and summer 133.

Texture masking unit 111 is responsive to summer 133. In this regard, as noted, texture masking unit 111 may put out a smaller weight value than the change in value that can be introduced into a pixel in the event that it receives a signal to that effect from

summer 133. More specifically, summer 133 adds the values supplied by texture masking unit 111 for each block. Summer 133 supplies as an output to texture masking unit 111 a maximum value that texture masking unit 111 can use as its output weight for the pixel currently being processed. The maximum value supplied by summer 133 is the lesser of the a) maximum weight value that can be accommodated by a pixel based on the texture surrounding it and b) the difference between a value supplied by bit mapper 123 to summer 133 for the block and the current sum for the block. Thus, once the sum equals the value supplied by bit mapper 123 to summer 133 for the block, texture masking unit 111 outputs a zero for each remaining pixel of the block.

Adder 115 produces a modified chrominance portion by adding the value supplied by multiplier 113 to the value of the portion of the chrominance which was selected by color selection 105 to carry the additional information for the pixel. As indicated, the portion of the chrominance that was selected by color selection 105 to carry the additional information is passed to adder 115 by double-pole, double-throw switch 109. The modified chrominance portion supplied by adder 115 is supplied to multiplexer 117.

Texture masking unit 111, multiplier 113, bit mapper 123 and summer 133 cooperate to effectively upsample the value being added to each pixel of the special processing resolution to match the format of the chrominance of the original video signal. To this end, the resulting upsampled values may be added to the selected chrominance portion of each pixel in the original video signal that corresponds to the location of a pixel in the special reduced resolution format used for processing. For example, if the original video signal is in 4-2-2 format, the values determined to be added to each of the pixels of a block in the special processing format are duplicated on a per-line basis so as to create a block of values to be added that has 8 pixels per line and 16 lines per block. In this block, each of the lines of the nonoverlapping groups of 2 consecutive lines has identical values to be added. Such a block corresponds in size to the original block of the selected chrominance portion of the original video in 4-2-2 format. Each value of the resulting upsampled block is added to the selected chrominance portion of the respective, like positioned pixel in the original video signal by adder 115. Those of ordinary skill in the art will readily be able to perform similar block conversions for different formats. Note that for those pixels of a block that color selection 105 did not determine that the selected chrominance portion could better accommodate a change, the value added will be zero. If the original video signal is in 4-2-0 format, no upsampling is required.

In another embodiment of the invention, only the decimated special processing resolution format is processed. The resulting modified chrominance portion is then

upsampled, e.g., in multiplexer 117. However, doing so may result in some degradation of the original video signal, although such degradation need not be visible.

Multiplexer 117 receives the original luminance component (Y) and the unmodified chrominance portion that was supplied from YUV demultiplexer and decimator 103 via double-pole, double-throw switch 109. Multiplexer 117 also receives the modified chrominance portion from adder 115. Multiplexer 117 then multiplexes together the original luminance component (Y), the unmodified chrominance portion, and the modified chrominance portion. Multiplexer 117 knows on which lead it receives the modified portion of the chrominance component and on which lead it receives the unmodified portion of the chrominance component by virtue of receiving the output of color selection 105. In accordance with an aspect of the invention, the resulting video signal is supplied as the watermarked output video signal.

Those of ordinary skill in the art will be able to develop embodiments of the invention in which the additional data is added to the original chrominance signal portion rather than the decimated version thereof, so that upsampling will not be required.

As indicated above, the binary data value, i.e., 1 or 0, of the additional information which is to be transmitted for each block may be supplied directly to bit mapper 123 for use as the watermark data or it may first be processed to facilitate the processing and recovery of the information at the receiver. Such exemplary processing may be performed by optional channel encoder 119 and block interleaver 121.

Channel encoder 119 receives the additional data that is desired to be embedded in the video stream. This data is then encoded, e.g., using a forward error correcting coding scheme. Such forward error correcting scheme may be any conventional forward error correcting scheme, such as convolutional encoding, e.g., Viterbi encoding or turbo encoding, or it may be any newly developed coding scheme. In one exemplary embodiment of the invention, convolutional coding of rate one-half is used. As a result of such coding, two bits are produced for every bit of the original bit stream. The channel encoded bit stream is supplied as an output by channel encoder 119 to block interleaver unit 121.

Block interleaver 121 rearranges the order of the bits of the channel encoded bit stream in order to randomly distribute the data. Doing so helps reduce the chance that adjacent sections of the channel encoded bit stream are lost, e.g., due to bursts of noise or other factors, which would then make it difficult to recover such data at the receiver from the remaining, actually received data. In an exemplary embodiment of the invention, the number of bits that are interleaved as a unit is equal to the number of blocks in a frame. A block interleaver may be implemented by writing data sequentially to the rows of a

block left to right, at the end of each row starting again at the leftmost position of the next row down, and then reading the data by starting at the leftmost topmost position of the block and reading down a column until the end of the column is reached at which point reading continues at the top of the next column. A block interleaver of 45 rows by 30 columns has proven effective for a picture size of 720 by 480 pixels. For different resolutions, those of ordinary skill in the art will be readily able to develop comparable block encoders. The interleaved channel encoded bit stream is supplied as an output by bit interleaver 121 to bit mapper 123.

In accordance with an aspect of the invention, the data bit supplied by block interleaver 121 is impressed as the watermark data, under the control of bit mapper 123, upon at least one block of at least one frame of the original video signal. In accordance with the principles of the invention, bit mapper 123 controls the insertion of the watermark data into one of the bit positions of the average value of at least a selected one of the chrominance portions of each block upon which the data is to be impressed, thus effectively replacing the bit at that bit position.

For example, when the watermark data is to be carried in the least significant bit of the integer portion of the average of the selected chrominance portion of the block, the value that needs to be added to the average value is 0 or 1. Zero is added when the least significant bit of the integer portion of the average value is already the same as the watermark data bit to be carried and 1 is added when the least significant bit of the integer portion of the average value is the complement of the watermark data bit to be carried. When the watermark data is to be carried in the second to the least significant bit of the integer portion of the average of the selected chrominance portion of the block, the value of the data to be added to the pixel is -1, 0, or 1. Zero is added when the second least significant bit of the integer portion of the average value is already the same as the watermark data bit to be carried and 1 or -1 is added when the second least significant bit of the integer portion of the average value is the complement of the watermark data bit to be carried. Whether 1 or -1 is added depends on which will cause the smallest change to the average value while changing the second least significant bit of the integer portion of the average value to its complement. Using the second to least significant bit the data to be embedded is more likely to survive encoding by MPEG or a similar process. When the data to be placed in the third to the least significant bit of the integer portion of the average of the selected chrominance portion of the block, the value of the data to be added to the pixel is -2, -1, 0, 1, or 2. Zero is added when the third least significant bit of the integer portion of the average value is already the same as the watermark data bit to be carried and is -2, -1, 1, or 2 is added when the third least significant bit of the integer

portion of the average value is the complement of the watermark data bit to be carried. Whether is -2, -1, 1, or 2 is added depends on which will cause the smallest change to the average value while changing the third least significant bit of the integer portion of the average value to its complement. Using the third to least significant bit the data to be
 5 embedded is even more likely to survive encoding by MPEG or a similar process to achieve adequate results. From the foregoing, those of ordinary skill in the art will readily be able to determine the values to be added for more significant bit positions which are determined by the user or the system.

To this end, bit mapper 123 develops a value that is distributively added to a
 10 selected chrominance portion of the pixels of a block such that doing so changes the average of the value of that chrominance portion for that block so that the bit supplied by block interleaver 121 that is being impressed is placed in a selected bit position of the average value of the selected chrominance portion. This value is the value to be added to the average value of the selected chrominance portion to place the watermark data bit in
 15 the appropriate bit position multiplied by the number of pixels in a block. In other words, the value developed by bit mapper 123 that is to be added to the average of the value of that chrominance portion is divided up into smaller values that are added to individual pixels of the block, so that the total of the smaller values added to the block divided by the number of pixels in the block equals the value to be added to the average value of the
 20 selected chrominance portion.

The particular bit average of the value of the chrominance portion for that block, e.g., the DC coefficient for that chrominance portion, onto which the data supplied by bit mapper 123 is impressed, is determined by bit mapper 123. In an exemplary embodiment of the invention, the second least significant bit of the DC coefficient for a block is
 25 replaced with the particular value that is desired to be impressed on the block. In another embodiment of the invention, which bit of the DC coefficient that is replaced may be a function of the texture variance of the block. It is advantageous to increase the significance of the bit which is replaced as the texture variance increases, because the MPEG coding standards employ greater quantization step sizes for higher texture
 30 variances, and the use of such greater quantization step sizes could filter out the watermark data bit if it is positioned in a bit position that is not significant enough. When using more significant bits, the values to be added or subtracted from the DC coefficient in order to change the bit being substituted to its complementary value may be greater than one. To this end, in accordance with an aspect of the invention, bit mapper 123
 35 receives the average variance of the luminance component for the block from texture masking 111, and based on the average variance, determines which bit position is to be

replaced. The greater the variance, the more significant the bit position into which the watermark data is placed.

Bit mapper 123 supplies the data bit from the interleaved channel encoded bit stream that is to be communicated for each block of the original video signal at the appropriate time for each pixel of the block of the original video signal when that pixel is to be incorporated into the watermarked output video signal. Thus, bit mapper 123 takes into account the fact that the processing of the video signal is line based, i.e., the processing is left to right on a line, then down to the next line and left to right again, causing the adjacent pixels of a block to not necessarily be located sequentially in the video stream and therefore to not all be processed in time directly one after the other. The particular data bit supplied as an output of bit mapper 123 at any time is supplied as an input to multiplier 113.

Using an encoder, such as shown in FIG. 1, a bit rate of around 6,750 bits per second, substantially error free, has been achieved for the additional information as supplied to channel encoder 119 when the video frame size is 720 x 480 pixels.

Those of ordinary skill in the art will readily recognize from the above description that various ones of the units in FIG. 1 require storage in order to first determine the values which must be computed using information from an entire block, e.g., the original average value of the block and the average texture variance of the block, and then to employ those values in processing the individual pixels. Consequently, there is typically a one slice delay, where a slice is a strip of blocks horizontally all the way across a frame.

FIG. 2 shows exemplary receiver 201 for recovering the additional data of a video signal containing digital watermarking on the chrominance signal thereof, in accordance with the principles of the invention. Shown in FIG. 2 are a) YUV demultiplexer (demux) and decimator 203, b) color selection unit 207, c) double pole double throw switch 209, d) block variance calculation 211, e) block integrator V 213, f) block integrator U 215, g) bit selection 217, h) deinterleaver 219, and i) channel decoder 221.

YUV demultiplexer and decimator 203, which may be substantially the same as YUV demultiplexer and decimator 103 of transmitter 101 (FIG. 1), receives a video signal that has been digitally watermarked in that additional information has been added thereto on the chrominance component of the signal, in accordance with the principles of the invention. YUV demultiplexer and decimator 203 works with digital video, e.g., formatted according to the serial digital interface (SDI). As will be recognized by those of ordinary skill in the art, any video signal not initially in an appropriate digital format may be converted thereto using conventional techniques.

YUV demultiplexer and decimator 203 demultiplexes the luminance (Y) component of the video and its chrominance component and decimates it to the preferred processing format in which for each original 2x2 luminance block of video, had the original block been in 4-4-4 representation, there remains only one Y, one U, and one V value. In order to know the format of the received video, a) the operator needs to indicate to YUV demultiplexer and decimator 203 the particular format of the input video, b) the format of the video may be detected directly from the video using conventional techniques, or c) the information may be supplied from a higher layer processor which is supplying the input video signal. The demultiplexed luminance and chrominance components are supplied to color selection 207. In addition, the luminance component is supplied to block variance calculation 211, the V chrominance portion is supplied to block integrator V 213, and the U chrominance portion is supplied to block integrator U 215. Unlike YUV demultiplexer and decimator 103, YUV demultiplexer and decimator 203 need not also supply a second set of YUV outputs in the full format of the original input video signal.

Color selection unit 207 determines for each block on which portion of the chrominance component, i.e., on the U portion or the V portion, it was likely that the additional information was embedded. The output of color selection unit 207 is used to control the position of double pole double throw switch 209. More specifically, color selection unit 209 selects the chrominance portion U or V, as a function of Y, U, and V, as will be described in more detail hereinbelow, on which the additional information was likely to have been embedded for this block. In one embodiment of the invention, color selection unit 207 is based on a lookup table. Doing so simplifies the process by avoiding the need for YUV to RGB conversion, which might otherwise be necessary.

Note that the input to color selection unit 207 is individual pixels. Color selection unit 207 keeps track of the pixels in each block and combines the individual U or V selection for each pixel in the block. The particular component that has the highest value, i.e., was most often selected for the pixels within a block, is determined to be the output of color selection 207. The output of color selection unit 207 is then set so that switch 209 supplies to bit selection 217 the integrated version of the portion of the chrominance component to which the additional data was determined to have been added.

Block variance calculation 211 determines the particular bit of the average of the value of the selected chrominance portion for that block, e.g., the DC coefficient for the selected chrominance portion, that likely contains the impressed data. As noted, in an exemplary embodiment of the invention, bit mapper 123 (FIG. 1) received and employed the average of the variances of the luminance component of the pixels of the block, to

determine which bit position is to be replaced with the watermark data bit to be impressed. The greater the variance, the more significant the bit position that should be replaced. Block variance calculation 211 (FIG. 2) should base its calculation on the same information used by mapper 123 to replicate its determination. The output of block variance calculation 211 is supplied to bit selection 217.

Block integrator V 213 integrates the values of V over a block, i.e., the values for each pixel in a block are combined, e.g., added together. Block integrator U 215 integrates the values of U over a block, i.e., the values for each pixel in a block are combined, e.g., added together.

Bit selection 217 extracts the bit at the bit position specified by block variance calculation 211 from the integrated chrominance portion value supplied to it by switch 209 as the data for the block.

Deinterleaver 219 reorders the data to undo the effect of block interleaver 121 (FIG. 1) of transmitter 101. The reordered values are then supplied to channel decoder 221 (FIG. 2), which performs appropriate decoding for a signal that was encoded using the type of encoding employed by channel encoder 119 of transmitter 101 (FIG. 1). The resulting decoded values are supplied by channel decoder 221 (FIG. 2) as the reconstructed version of the additional data signal. For further robustness, channel decoder 221 may be a so-called "sequence decoder", e.g., a turbo decoder.

FIGs. 3A and 3B, when connected together as shown in FIG. 3, show an exemplary process for use in watermarking one of the chrominance portions with additional data, in accordance with the principles of the invention. For those blocks where the determined bit position is already the same as the value to be impressed, the block may be transmitted unmodified. The process of FIG. 3 may be performed, in an exemplary embodiment of the invention, in a system such as is shown in FIG. 1.

The process may be entered in step 301 when all the pixels of a block are available. Part of the processing of FIG. 3 takes place on a block-by-block basis, and part on a pixel-by-pixel basis. The blocks of a frame are indexed using a two-dimensional pointer p, q , where p points to the particular horizontal slice of the frame that is being processed and q points to the particular column, or vertical slice, of the frame. For example, for 720x480 resolution p ranges between 1 and 30 and q between 1 and 45. Similarly, the pixels of each block are indexed using a two-dimensional pointer i, j , where i points to the particular row within the block that is being processed and j points to the particular column within the block that is being processed. For example, in the special processing mode employed to impress the data, where each macroblock of original video has only a corresponding 8x8 block of Y, U, and V, both i and j range between 0 and 7.

After entering the process in step 301, several variables that are used in the process are initialized in step 303, e.g., $\text{countU}(p,q)=0$, $\text{countV}(p,q)=0$, $\text{sumU}(p,q)=0$, $\text{sumV}(p,q)=0$, and $\text{var}(p,q)=0$. CountU is a running total of how many pixels within the block are selected by the color selection process as being suitable for watermarking on the U chrominance portion while count V is a running total of how many pixels within the block are selected by the color selection process as being suitable for watermarking on the V chrominance portion. SumU and sumV are the running total values of U and V respectively over all the pixels of the block. In embodiments of the invention where watermarking is only performed only on pixels of the chrominance portion selected for the block, there is no use for the one of sumU and sumV that is developed for the chrominance portion that is not selected.

In step 305, $\text{var}(p,q)$, the total of the variance of the luminance for each individual pixel within the block, which is, of course, proportional to the average variance of the luminance for the block, is computed. To this end, i and j are initially both set to point to the first pixel of the block to be processed, e.g., $i=0$ and $j=0$. The value of $\text{var}(p,q)$, is computed by cycling through each pixel of the block, changing the values of i and j as appropriate to do so, and adding together the variance of the luminance for each pixel to the current total of $\text{var}(p,q)$.

In one embodiment of the invention, the variance of the luminance for any particular pixel may computed by taking the absolute value of the difference in the luminance between the pixel and all of its nearest neighbors. Mathematically, where all of the nearest neighbors are within the same block, this may be written as

$$\text{var}(p,q)=\text{var}(p,q)+(|Y_{(i,j)}^{(p,q)}-Y_{(i-1,j-1)}^{(p,q)}|+|Y_{(i,j)}^{(p,q)}-Y_{(i-1,j)}^{(p,q)}|+|Y_{(i,j)}^{(p,q)}-Y_{(i,j-1)}^{(p,q)}|+|Y_{(i,j)}^{(p,q)}-Y_{(i,j)}^{(p,q)}|+|Y_{(i,j)}^{(p,q)}-Y_{(i+1,j-1)}^{(p,q)}|+|Y_{(i,j)}^{(p,q)}-Y_{(i+1,j)}^{(p,q)}|+|Y_{(i,j)}^{(p,q)}-Y_{(i,j+1)}^{(p,q)}|+|Y_{(i,j)}^{(p,q)}-Y_{(i-1,j+1)}^{(p,q)}|+|Y_{(i,j)}^{(p,q)}-Y_{(i+1,j+1)}^{(p,q)}|).$$

Those of ordinary skill in the art will readily be able to adapt the foregoing to those pixels whose nearest neighbors are in other blocks. Furthermore, for those blocks that are near the borders of the frame, and hence have no nearest neighbors, or the nearest neighbors are part of those blocks that are not displayed, the value of such neighbors may be considered to be zero.

In accordance with another aspect of the invention, not all of a pixel's nearest neighbors need be considered in the variance computation and yet sufficiently high quality results can be achieved. More specifically, it is advantageous in that computation time for each pixel is reduced by taking only the differences of the 4 pixels in the corners of the rectangle surrounding the pixel and 2 of the other pixels that form a vertical or horizontal line with the pixel, e.g., the 2 pixels on the horizontal line with the pixel.

Thereafter, conditional branch point 307 tests to determine which particular chrominance portion, i.e., U or V, is going to contain the watermark information for the block. This is done by evaluating the color selection for each pixel in the block and counting the number of pixels within the block that are selected for each chrominance portion. The chrominance portion that was selected the most for the block is chosen for watermarking. Note that in some embodiments of the invention, it may be determined that a particular pixel is unsuitable for watermarking at all. In such a case, it is not counted towards the total number of pixels for either U or V.

The particular method of determining the color selected to be watermarked for each pixel is at the discretion of the implementer. In one embodiment of the invention, the chrominance portion of the pixel with the smallest value is selected. In another embodiment of the invention, the color selection arrangement described hereinbelow is employed.

Next, the bit position of the average value of the selected chrominance portion that will contain the watermarked bit is determined. The bit position is selected so that the watermarked bit will survive any subsequent quantization, such as takes place in MPEG-like encoding.

To this end, if the test result in step 307 is that the V chrominance portion is selected to be watermarked, control passes to step 309, in which a variable *watermarkcolor* is set equal to V. Thereafter, conditional branch point 323, which tests to determine whether the average Y variance over the block, $\text{var}(p,q)$, is greater than a first prescribed V threshold $t1v$, which is the largest V threshold. An exemplary value of $t1v$ is 600.

Note that the particular threshold values used in connection with FIGs. 3 and 4 for both U and V are at least partially dependent on the number of bits used to represent each Y value, when the average Y variance is compared with the suggested threshold. For example, the suggested threshold values herein are for Y being an 8 bit value. Those of ordinary skill in the art will readily recognize that the values employed for 8 bits may be scaled to 10 bits by multiplying by 4, e.g., shifting the value to the left two times. Likewise, other numbers of bits used for Y, U, and V can be similarly accommodated.

In other embodiments of the invention, instead of using the average Y variance over the block for the various comparisons, a different average variance, e.g., the average V variance over the block, may be calculated and employed.

If the test result in step 323 is YES, indicating that the variance is large enough that the additional data should be encoded on the 5th least significant bit of the average of the V values of the pixels of the block, e.g., the value of $\text{int}[\text{sum}V(p,q)/(\text{number of pixels})]$

per block]], e.g., $\text{int}[\text{sumV}(p,q)/64]$, is greater than $t1v$, control is passed to step 325, in which a variable m is set equal to 5.

Note that instead of using the integer function int for rounding, as is used herein, any other form of rounding to achieve an integer value may be employed, e.g., always rounding up or always rounding to the nearest integer value.

If the test result in step 323 is NO, indicating that the variance was not large enough that additional the data should be encoded on the 5th least significant bit of the average value of the V values of the pixels of the block, control passes to conditional branch point 329, which tests to determine if the average Y variance over the block, $\text{var}(p,q)$, is greater than a second prescribed V threshold, $t2v$, which is the second largest V threshold. An exemplary value of $t2v$ is 15.

If the test result in step 329 is YES, indicating that the additional data should be encoded on the 4th least significant bit of the average of the V values of the pixels of the block, control is passed to step 331, in which variable m is set equal to 4.

If the test result in step 329 is NO, indicating that the variance was not large enough that the additional data should be encoded on the 4th least significant bit of the average of the V values of the block, control passes to conditional branch point 333, which tests to determine if the average Y variance over the block, $\text{var}(p,q)$, is greater than a third prescribed V threshold, $t3v$, which is the smallest V threshold. An exemplary value of $t3v$ is 7.

If the test result in step 333 is YES, indicating that the variance is large enough that the data should be encoded on the 3rd least significant bit of the average of the V values of the pixels of the block, control is passed to step 335, in which variable m is set equal to 3.

If the test result in step 333 is NO, indicating that the variance is only large enough that the data should be encoded on the 2nd least significant bit of the average value of the V value of the block control is passed to step 337, in which variable m is set equal to 2.

If the test result in step 307 is that the U is the chrominance portion is selected to be watermarked, control passes to step 311, in which the variable *watermarkcolor* is set equal to U. Thereafter, conditional branch point 343 tests to determine whether the average Y variance over the block, $\text{var}(p,q)$, is greater than a first prescribed threshold $t1u$, which is the largest threshold. An exemplary value of $t1u$ is 600.

In other embodiments of the invention, instead of using the average Y variance over the block for the various comparisons, the average U variance over the block may be calculated and employed.

If the test result in step 343 is YES, indicating that the variance is large enough that the data needs to be encoded on the 5th least significant bit of the average of the U values of the pixels of the block, e.g., the value of $\text{int}[\text{sum}V(p,q)/(\text{number of pixels per block})]$, e.g., $\text{int}[\text{sum}U(p,q)/64]$, is greater than $t1u$, control is passed to step 345, in which variable m is set equal to 5.

Note that instead of using the integer function int for rounding herein, any other form of rounding to achieve an integer value may be employed, e.g., always rounding up or rounding to the nearest integer value.

If the test result in step 343 is NO, indicating that the variance was not large enough that the data needed to be encoded on the 5th least significant bit of the average of the U values of the pixels of the block, control passes to conditional branch point 349, which tests to determine if the average Y variance over the block, $\text{var}(p,q)$, is greater than a second prescribed threshold $t2u$, which is the second largest U threshold. An exemplary value of $t2u$ is 15.

If the test result in step 349 is YES, indicating that the data needs to be encoded on the 4th least significant bit of the average of the U values of the pixels of the block, control passes to step 351, in which variable m is set equal to 4.

If the test result in step 349 is NO, indicating that the variance was not large enough that the data should be encoded on the 4th least significant bit of the average of the U value of the pixels of the block, control passes to conditional branch point 353, which tests to determine if the average Y variance over the block, $\text{var}(p,q)$, is greater than a third prescribed threshold $t3u$, which is the smallest U threshold. An exemplary value of $t3u$ is 7.

If the test result in step 353 is YES, indicating that the variance is large enough that the data should be encoded on the 3rd least significant bit of the average of the U values of the pixels of the block, control passes to step 355, in which variable m is set equal to 3.

If the test result in step 353 is NO, indicating that the variance is only large enough that the data should be encoded on the 2nd least significant bit of the average of the U values of the pixels of the block, control is passed to step 357, in which variable m is set equal to 2.

Once the particular bit of the average value over the block of the selected chrominance portion to be employed to contain the watermarked data is determined, the process to make certain that that bit position contains the desired bit is undertaken. The goal of the process is to add or subtract the minimum possible value from the current average value of the selected chrominance portion to make certain that the desired bit

position has the value of the watermarking bit to be transmitted. Note that, in one embodiment of the invention, the desired bit position is a bit position within the integer portion of the average value. To this end, ideally, if the desired bit position already contains the value of the watermarking bit to be transmitted, nothing may be added to the current average value of the selected chrominance portion. On the other hand, if the desired bit position contains the complement of the value of the watermarking bit to be transmitted, ideally, only the smallest possible value that will flip the desired bit position to its complement by being either added to or subtracted from the desired bit position, and hence causing the least change in the value of the average value of the selected chrominance portion from its current unwatermarked value to its final watermarked value, is added to or subtracted from the desired bit position as appropriate.

In practice, due to quantization noise, rounding as part of the inventive process, and other factors of the MPEG-like encoding process that may impact the final value of the desired bit, a slightly different value may be added or subtracted as explained further herein. More specifically, in one embodiment of the invention, a “safe” range of values having the desired bit value at the desired bit position is selected, and the minimum value is either added or subtracted to the average value of the selected chrominance portion so that the final value has the desired bit value at the desired bit position and it is within the safe range. Thus, typically, whenever a bit of the average value needs to be changed to its complement to carry the watermark data, the resulting value is always at the border of a safe range. When the value at the desired bit position is already the value of the watermark data bit to be transmitted, if the average value of the selected chrominance portion is already within the safe range, then nothing needs to be added to the average value of the selected chrominance portion. However, when the average value of the selected chrominance portion is not already within the safe range, then the minimum value necessary to change the average value of the selected chrominance portion to be a value within the safe range, while keeping the value of the desired bit position at the value of the watermarking bit to be transmitted, is added to, or subtracted, from the average value of the selected chrominance portion.

Conceptually, the foregoing may be thought of as first adding or subtracting the minimum value to achieve the desired watermarking value at the desired bit position, and then adding or subtracting a further amount, e.g., a margin value, to insure that the final value is within the safe range.

FIG. 5 shows an example of several safe ranges where the desired bit position is the third least significant bit. Along the axis are shown the average value of the selected chrominance portion

Table 1 shows (code) (table of values)

Upon completion of steps 325, 331, 335, 337, 345, 351, 355 and 357, control passes to conditional branch point 361, which tests to determine if the bit of watermarking data to be impressed on the block is the same as the current identified bit position for the average value of the chrominance portion identified by the variable *watermarkcolor*. If the test result in step 361 is YES, indicating that the bit of watermarking data to be impressed on the block is the same as the current identified bit position for the average value of the chrominance portion identified by the variable *watermarkcolor*, and that therefore the bit does not need to be changed to its complementary value, control passes to step 363, which tests to determine if the value is within the safe range for the current bit position. If the test result is NO, indicating that an error might be introduced during subsequent processing, control passes to step 365, which sets the variable *changevalue* to be equal to the value needed to move the current average value for the color indicated by *watermarkcolor* into the nearest safe range without changing the value of the desired bit position. Note that the value need not be an integer value, and it may also be a negative value. If the test result in step 363 is NO, indicating that the current average value for the color indicated by *watermarkcolor* is already within a safe range, control passes to step 367, and the value of *changevalue* is set equal to zero.

If the test result in step 361 is NO, indicating that the bit of watermarking data to be impressed on the block is not the same as the current identified bit position for the average value of the chrominance portion identified by the variable *watermarkcolor*, and that therefore the value of the bit must be changed to its complementary value so as to properly carry the watermarking data, control passes to step 369, which tests to determine if the nearest safe range for the current bit position is greater or smaller than the current average value of the color indicated by *watermarkcolor*. If the test result in step 369 is GREATER, indicating that the values of the nearest safe range for the current bit position is greater than the current average value of the color indicated by *watermarkcolor*, control passes to step 371 in which the value of variable *changevalue* is set equal to the smallest value to add to the average value so that the resulting value is within the adjacent safe range with bigger values. Note that this value need not be an integer value. If the test result in step 369 is SMALLER, indicating that the values of the nearest safe range for the current bit position is smaller than the current average value of the color indicated by *watermarkcolor*, control passes to step 373 in which the value of variable *changevalue* is set equal to the smallest negative value that when added to the average value results in a

value that is within the adjacent safe range with smaller values. Again, note that this value need not be an integer value, and it may also be a negative value.

Upon conclusion of step 365, 367, 371, or 373, control passes to step 375 in which the total to add to the pixels is set equal to the product of the number of pixels per block and the value of *changevalue*. If the resulting product value is not an integer, the value is rounded off. The rounding may be performed in a manner consistent with the steps 365, 371, and 373, in that if a negative value was added, the rounding is down by taking the integer portion of the value, while if a positive value was added the rounding is up toward the next whole integer value.

Processing now changes from a per-block level to a per-pixel level within the block. In step 377, the first pixel of the block is pointed to. Thereafter, conditional branch point 379 tests to determine if the current pixel is to be watermarked, based on its color. This is done by determining if the chrominance component of this pixel that is suitable for watermarking is the same as the color selected in step 307 for the entire block. If the test result in step 379 is YES, indicating that this pixel should be watermarked, control passes to step 381, in which a value is added to the current pixel based on the luminance variance for the pixel and the total values added so far to the pixels of the block.

More specifically, a maximum value that can be added to the pixel without introducing a visible artifact is determined as a function of the variance of the luminance. The greater the variance of the luminance, the greater the value that can be added, up to a prescribed maximum. Note that this value may be positive or negative. This value is then added to pixel if the total to be added to the pixels is a positive value, or the value is subtracted from the pixel if the total to be added to the pixels is a negative value. However, as the per-pixel processing proceeds running total of the values added or subtracted are subtracted from the total to be added to the pixels. If the value to be added to the current pixel will make the difference between the total to be added to the pixels and the running total cross zero, then the value is adjusted so that the running total just equals zero.

If the test result in step 379 is NO, or after completing step 381, control passes to conditional branch point 383, which tests to determine if the current pixel is the last pixel of the block. If the test result in step 383 is NO, control passes to step 385 which tests to determine if the total to be added to the pixels of the block has already been added, i.e., is the running total equal to the total to be added to the pixels of the block. If the test result in step 385 is NO, indicating that there is more that needs to be added to the pixels of the

block, control passes to step 387, which points to the next pixel of the block. Control then passes back to step 379, and the process continues as described above.

If the test result in either of steps 383 or 385 is YES, indicating that either all the pixels of the block have been processed or all of the total that need to be added has been added, control passes to step 389 and the process is exited.

FIGs. 4A and 4B, when connected together as shown in FIG. 4, show an exemplary process for extracting the additional information from a digitally watermarked video signal in which the additional information that constitutes the watermarking signal within the video signal has been impressed upon the chrominance component, in accordance with the principles of the invention. Such a process may be implemented by an exemplary embodiment of the invention, such as the one shown in FIG. 2, across color selection 207, double pole double throw switch 209, block variance calculation 211, block integrator V 213, block integrator U 215 and bit selection 217 (FIG. 2).

The process is entered in step 401 (FIG. 4) when a new block of the received decimated frame is to be processed. Note that for pedagogical purposes it is assumed herein that pixels are supplied for processing by the process of FIG. 4 grouped by block, so that all the pixels of a block are processed prior to any pixels of the next block being processed. However, in designing an actual system, those of ordinary skill in the art will readily recognize that the pixels may be processed in the same order that they are scanned and that appropriate memory locations and control structures may be used so as to effectively separately process the blocks.

Part of the processing of FIG. 4 takes place on a block-by-block basis, and part on a pixel-by-pixel basis. The blocks of a frame are indexed using a two-dimensional pointer p,q , where p points to the particular horizontal slice of the frame that is being processed and q points to the particular column, or vertical slice, of the frame. For example, for 720x480 resolution, p ranges between 1 and 30 and q between 1 and 45. Similarly, the pixels of each block are indexed using a two-dimensional pointer i,j , where i points to the particular row within the block that is being processed and j points to the particular column within the block that is being processed. For example, in the special processing mode employed to impress the data, where each macroblock of original video has only a corresponding 8x8 block of Y, U, and V, both i and j range between 0 and 7.

After entering the process in step 401, several variables that are used in the process are initialized in step 403, e.g., $\text{countU}(p,q)=0$, $\text{countV}(p,q)=0$, $\text{sumU}(p,q)=0$, $\text{sumV}(p,q)=0$, and $\text{var}(p,q)=0$. CountU and countV are a running total of how many pixels within the block were selected by the color selection process as being U and V, respectively, while sumU and sumV are the running total values of U and V, respectively,

over all the pixels of the block. For the block, i and j are both set to point to the first pixel of the block to be processed, e.g., $i=0$ and $j=0$ as well. For each block, $\text{var}(p,q)$ represents the total of the variance of the luminance for each individual pixel within the block, which is, of course, proportional to the average variance of the luminance for the block.

Thereafter, in step 405, the Y, U and V values for the currently pointed to pixel of the currently being processed block is obtained, e.g., the values of $Y_{(i,j)}^{(p,q)}$, $U_{(i,j)}^{(p,q)}$, and $V_{(i,j)}^{(p,q)}$ are obtained. The current values of U and V are added to the respective current values of sumU and sumV in step 407. Also in step 407 the variance of the luminance, $\text{var}(p,q)$, is updated by adding the variance of the luminance for the current pixel to the current total of $\text{var}(p,q)$. In one embodiment of the invention, the variance of the luminance for the current pixel may be computed by taking the absolute value of the difference in the luminance between the current pixel and all of its nearest neighbors. Mathematically, where all of the nearest neighbors are within the same block this may be written as

$$\text{var}(p,q) = \text{var}(p,q) + (|Y_{(i,j)}^{(p,q)} - Y_{(i-1,j-1)}^{(p,q)}| + |Y_{(i,j)}^{(p,q)} - Y_{(i-1,j)}^{(p,q)}| + |Y_{(i,j)}^{(p,q)} - Y_{(i,j-1)}^{(p,q)}| + |Y_{(i,j)}^{(p,q)} - Y_{(i,j)}^{(p,q)}| + |Y_{(i,j)}^{(p,q)} - Y_{(i+1,j+1)}^{(p,q)}| + |Y_{(i,j)}^{(p,q)} - Y_{(i+1,j)}^{(p,q)}| + |Y_{(i,j)}^{(p,q)} - Y_{(i,j+1)}^{(p,q)}| + |Y_{(i,j)}^{(p,q)} - Y_{(i-1,j+1)}^{(p,q)}| + |Y_{(i,j)}^{(p,q)} - Y_{(i+1,j-1)}^{(p,q)}|).$$

Those of ordinary skill in the art will readily be able to adapt the foregoing to those pixels whose nearest neighbors are in other blocks. Furthermore, for those blocks that are near the borders of the frame, and hence have no nearest neighbors, or the nearest neighbors are part of those blocks that are not displayed, the value of such neighbors may be considered to be zero.

In accordance with another aspect of the invention, not all of the nearest neighbors need be considered and yet sufficiently high quality results can be achieved. More specifically, it is advantageous in that computation time is reduced to take the differences of the 4 pixels in the corners of the rectangle surrounding the current pixel and 2 of the other pixels that form a vertical or horizontal line with the current pixel, e.g., the 2 pixels on the horizontal line with the current pixel. However, the decoder should match the same process that was employed in the encoder.

Control passes to conditional branch point 409, which tests to determine on which of U or V it was likely that the additional data was impressed. The details of this determination will be described further hereinbelow. If the test result in step 409 is U, indicating that the additional data was most likely impressed on U for the current pixel, control passes to step 411, in which countU is incremented. Control then passes to step 413. If the test result in step 409 is V, indicating that the additional data was most likely

impressed on V for the current pixel, control passes to step 415, in which countV is incremented. Control then passes to step 413.

In some embodiments of the invention, conditional branch point 409 may be a three-way test, with an additional result indicating that it is likely that data was not
 5 impressed on the pixel at all, i.e., not on the U or the V. If such is the result, control simply passes directly to step 413.

Conditional branch point 413 tests to determine if the current pixel is the last pixel of the current block. If the test result in step 413 is NO, indicating that there remains additional pixels in the current block that have yet to be processed, control passes to step
 10 417, in which the values of i and j are adjusted to point to the next as-of-yet-not-processed pixel. Control then passes back to step 405 and the process continues as described above. If the test result in step 413 is YES, indicating that all the pixels of the current block have been processed, control passes to step 419, in which the variance of the decimated luminance for the block is calculated, i.e., the variance of the 8x8 Y block
 15 is calculated.

Control then passes to conditional branch point 421, which tests to determine if $\text{countV} > \text{countU}$ for the current block. If the test result in step 421 is that countV is indeed greater than countU, control passes to conditional branch point 423, which tests to
 20 determine whether the average Y variance over the block, $\text{var}(p,q)$, is greater than a first prescribed threshold $t1v$, which is the largest V threshold. An exemplary value of $t1v$ is 600.

In other embodiments of the invention, instead of using the average Y variance over the block for the various comparisons, the average U or the average V variance over the block may be calculated and employed, e.g., whichever has the greater count value.

If the test result in step 423 is YES, indicating that the variance is large enough
 25 that the data was likely to have been encoded on the 5th least significant bit of the integer portion of the average of the V values of the pixels of the block, e.g., the value of $\text{int}[\text{sumV}(p,q)/(\text{number of pixels per block})]$, e.g., $\text{int}[\text{sumV}(p,q)/64]$, control is passed to step 425, in which a variable m is set equal to 5. Control then passes to step 427, in
 30 which the value of the m^{th} least significant bit of the average of the V values of the pixels of the block is extracted as the value impressed upon this block. The process is then exited in step 459.

Note that instead of using the integer function int for rounding herein, any other
 35 form of rounding to achieve an integer value may be employed, e.g., always rounding up or rounding to the nearest integer value.

If the test result in step 423 is NO, indicating that the variance was not large enough that the data was likely to have been encoded on the 5th least significant bit of the integer portion of the average of the V values of the pixels of the block, control passes to conditional branch point 429, which tests to determine if the average Y variance over the block, $\text{var}(p,q)$, is greater than a second prescribed threshold $t2v$, which is the second largest V threshold. An exemplary value of $t2v$ is 15.

If the test result in step 429 is YES, indicating that the variance is large enough that the data was likely to have been encoded on the 4th least significant bit of the integer portion of the average of the V values of the pixels of the block, control is passed to step 431, in which variable m is set equal to 4. Control then passes to step 427, in which the value of the m^{th} least significant bit of the average of the V values of the pixels of the block is extracted as the value impressed upon this block. The process is then exited in step 459.

If the test result in step 429 is NO, indicating that the variance was not large enough that the data was likely to have been encoded on the 4th least significant bit of the integer portion of the average of the V values of the pixels of the block, control passes to conditional branch point 433, which tests to determine if the average Y variance over the block, $\text{var}(p,q)$, is greater than a third prescribed threshold $t3v$, which is the smallest V threshold. An exemplary value of $t3v$ is 7.

If the test result in step 433 is YES, indicating that the variance is large enough that the data was likely to have been encoded on the 3rd least significant bit of the integer portion of the average of the V values of the pixels of the block, control is passed to step 435, in which variable m is set equal to 3. Control then passes to step 427, in which the value of the m^{th} least significant bit of the average of the V values over the pixels of the block is extracted as the value impressed upon this block. The process is then exited in step 459.

If the test result in step 433 is NO, indicating that the variance is only large enough that the data was likely to have been encoded on the 2nd least significant bit of the integer portion of the average of the V values of the pixels of the block, control is passed to step 437, in which variable m is set equal to 2. Control then passes to step 427, in which the value of the m^{th} least significant bit of the average of the V values of the pixels of the block is extracted as the value impressed upon this block. The process is then exited in step 459.

If the test result in step 421 is that countU is greater than countV, control passes to conditional branch point 445, which tests to determine whether the average Y variance

over the block, $\text{var}(p,q)$, is greater than a first prescribed threshold $t1u$, which is the largest U threshold. An exemplary value of $t1u$ is 600.

If the test result in step 445 is YES, indicating that the variance is large enough that the data was likely to have been encoded on the 5th least significant bit of the integer portion of the average of the U values of the block, e.g., the value of
 5 $\text{int}[\text{sum}U(p,q)/(\text{number of pixels per block})]$, e.g., $\text{int}[\text{sum}U(p,q)/64]$, control is passed to step 445, in which variable m is set equal to 5. Control then passes to step 447, in which the value of the m^{th} least significant bit of the average of the U values over the pixels of the block is extracted as the value impressed upon this block. The process is then exited
 10 in step 459.

If the test result in step 445 is NO, indicating that the variance was not large enough that the data was likely to have been encoded on the 5th least significant bit of the integer portion of the average of the U values of the pixels of the block, control passes to conditional branch point 449, which tests to determine if the average Y variance over the
 15 block, $\text{var}(p,q)$, is greater than a second prescribed threshold $t2u$, which is the second largest U threshold. An exemplary value of $t2u$ is 15.

If the test result in step 449 is YES, indicating that the variance is large enough that the data was likely to have been encoded on the 4th least significant bit of the integer portion of the average of the U values of the block, control is passed to step 451, in which
 20 a variable m is set equal to 4. Control then passes to step 447, in which the value of the m^{th} least significant bit of the average of the U values of the pixels of the block is extracted as the value impressed upon this block. The process is then exited in step 459.

If the test result in step 449 is NO, indicating that the variance was not large enough that the data was likely to have been encoded on the 4th least significant bit of the integer portion of the average of the U values of the pixels of the block, control passes to
 25 conditional branch point 453, which tests to determine if the average Y variance over the block, $\text{var}(p,q)$, is greater than a third prescribed threshold $t3u$, which is the smallest U threshold. An exemplary value of $t3u$ is 7.

If the test result in step 453 is YES, indicating that the variance is large enough
 30 that the data was likely to have been encoded on the 3rd least significant bit of the integer portion of the average of the U values of the pixels of the block, control is passed to step 455, in which variable m is set equal to 3. Control then passes to step 447, in which the value of the m^{th} least significant bit of the average of the U values of the pixels of the block is extracted as the value impressed upon this block. The process is then exited in
 35 step 459.

If the test result in step 453 is NO, indicating that the variance is only large enough that the data was likely to have been encoded on the 2nd least significant bit of the integer portion of the average of the U values of the pixels of the block, control is passed to step 457, in which variable m is set equal to 2. Control then passes to step 447, in which the value of the m^{th} least significant bit of the average value of the U values of the pixels of the block is extracted as the value impressed upon this block. The process is then exited in step 459.

Note that although the use of 3 thresholds and 4 bit positions has been shown in FIGs. 3 and 4, those of ordinary skill in the art will readily be able to adapt the indicated method to other numbers of thresholds and encoded values.

Similarly, not all blocks of each frame or field of the video signal need be impressed with additional information.

FIG. 6 shows an exemplary process for determining which particular chrominance portion is more suitable, and so should be selected, to contain the watermarking information for a pixel, in accordance with the principles of the invention. The process is entered in step 601 when it is necessary to select a chrominance portion to contain watermarking information. For purposes of discussion of FIG. 6, it is assumed that the pixel is represented in YUV format. Furthermore, it is noted that, preferably, for each original 2x2 luminance block of original video, had the original video been in 4-4-4 representation, there should only one Y value for each chrominance component, i.e., each pair of respective corresponding U and V values. To this end, the Y values of the original block may be downsampled so as to have the same resolution as the U and V. Alternatively, the average, or some other combination, of the Y values associated with a particular U and V values may be computed and used as the Y value for the process of FIG. 6.

Conceptually, in accordance with the principles of the invention, each position in a three-dimensional YUV colorspace corresponding to a possible pixel position, given the full range that a pixel's Y, U, and V values can take, is assigned a chrominance portion, e.g., based on experimental observations, that is more suitable, and so should be selected, for a pixel having such Y, U, and V values. If a version of the entire table for each possible set of Y, U, and V values was to be employed, where each of Y, U, and V has a full range of 8 bits, at least 16M bit of information would need to be stored, assuming that only one bit was stored for each position to indicate the selected chrominance portion. Note that use of a single bit only permits selection of U or V, but not a designation that neither U nor V should be employed. If it were desired to be able to select neither U nor V, 32 Mbits of information would be necessary.

A cutaway view of a portion of exemplary assignments of a chrominance portion that is to be selected for each possible pixel within a three-dimensional YUV colorspace is shown in FIG. 7. Note that FIG. 7 is provided for pedagogical purposes only, as a conceptualization visual aid, and does not represent actual data.

5 In order to reduce the storage requirements, the YUV colorspace may be considered to be a group of regions, each region being defined to include the positions corresponding to at least one set, and typically multiple sets, of Y, U, and V values, i.e., the positions in the colorspace corresponding to at least one pixel, and possibly many pixels, and each region, and hence each pixel which maps to that region, is assigned a
10 chrominance portion, e.g., based on experimental observations, that is to be selected for any pixel whose set of Y, U, and V values fall within the region. One way to look at such grouping into regions is a quantization, which may be linear or nonlinear.

Table 1 is a listing for an exemplary colorspace selection table, where each region corresponds to 4 Y values, 4 U values, and 4 V values, and hence to 64 possible
15 combinations of 8 bit values for any pixel. Using such a table reduces the required information to be stored down to 256 Kbits, assuming that only one bit was stored for each position, or 512 Kbits, assuming it were desired to be able to select Y, V, and neither U nor V. Table 1 may be stored in any computer readable medium, e.g., ROM, RAM, magnetic storage such as a hard disk or tape drive, optical storage such as a CD-
20 ROM or DVD-ROM, or the like.

Those of ordinary skill in the art will readily recognize that the values employed in Table 1, which are for each of Y, U, and V having a full range of 8 bits, may be scaled for use with 10 bit Y, U, and V values by dividing by 4, e.g., shifting each 10 bit value to the right two times. Likewise, other numbers of bits used for Y, U, and V can be
25 similarly accommodated.

In order to effectively arrange and access the data of Table 1, it is arranged so that the specified U or V selection, where 1 indicates select U and 0 indicates select V, for 8 adjacent regions having the same U and V quantized values but different sequential quantized Y values, are grouped together to form a byte. Thus, for each U and V value
30 there are 8 bytes, each corresponding to a region having the same U and V quantized values but different quantized Y values.

Table 1 is arranged to be addressed using an address that has the most significant bits corresponding to the U values, the next least significant values corresponding to the V values, and the least significant values corresponding to the Y values. In other words,
35 the address of the bytes may be formed as follows:

$$U7|U6|U5|U4|U3|U2|V7|V6|V5|V4|V3|V2|Y7|Y6|Y5$$

where U7,U6,U5,U4,U3, and U2 are the values of the 8th to 3rd least significant bits of the pixels U value, V7,V6,V5,V4,V3, and V2 are the values of the 8th to 3rd least significant bits of the pixels V value, and Y7,Y6, and Y5, are the values of the 8th to 6th least significant bits of the pixels Y value. Then, the particular bit within the byte is
 5 specified by using the 5th to 2nd least significant bits of the Y component, e.g., Y4,Y3, and Y2.

A table such as Table 1 is reflective of the facts that the human visual system is a) less sensitive to the blue color and b) more sensitive to lower luminance values. Such a table may be developed by trial and error, generally as follows.

10 The colorspace is examined in sections, each section being defined by a luminance value and ranging in a first dimension corresponding to a first chrominance portion changing from its minimum value to its maximum value and in the second dimension corresponding to the second chrominance portion changing from its minimum value to its maximum value. Any or all of the luminance and the chrominance portions
 15 may be quantized, e.g., using the 6 most significant bits of 8 bit values. Doing so creates a set of planes having a checkerboard of chrominance portion values, which appears when displayed as blocks of different colors, one plane for each luminance value. For example, quantizing so as to use the 6 most significant bits of 8 bit values for the luminance and both chrominance portions yields 64 planes that correspond to each possible quantized
 20 luminance value, and each plane has a checkerboard pattern of colored boxes, with 64 boxes vertically and 64 boxes horizontally for a total of 4096 boxes per plane.

Each plane is examined separately. Random data is developed for a number of frames sufficient to be confident that the random data will have different values in like positioned blocks of the frame over time and for an observer to detect flicker should it
 25 appear. Thirty seconds or longer have proven to be of value. The random data is impressed upon frames that contain the plane, but only on a first one of the chrominance portions, e.g., using the system of FIG. 1 and the process of FIG. 3 to accomplish the watermarking but forcing the color selection to be the first chrominance portion. The resulting watermarked version of the frames is displayed and observed.

30 Any block for which no flicker is observed is indicated in the table that its combination of luminance and chrominance portions should employ the chrominance portion currently carrying the watermark data as the selected chrominance portion for that combination. Any block for which flicker is observed is indicated in the table that its combination of luminance and chrominance portions should employ the chrominance
 35 portion that is not currently carrying the watermark data as the selected chrominance

portion for that combination. The process is repeated for the plane but changing the chrominance portion that is watermarked.

For any block of a plane that flicker occurs for both chrominance portions, as can happen, the implementer may choose which chrominance portion should be selected. For example, U may be chosen because the human visual system is generally less sensitive to blue. Alternatively, the chrominance portion that would provide for better data compression of the resulting table may be employed. Similarly, where flicker does not appear on either block, the choice of the chrominance portion to employ is at the discretion of the implementer.

The process is repeated for each plane until the entire table is populated.

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	3105 to 3120	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	3121 to 3136	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	3137 to 3152	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
5	3153 to 3168	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	3169 to 3184	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	3185 to 3200	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	3201 to 3216	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	3217 to 3232	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
10	3233 to 3248	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	3249 to 3264	0	0	8	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	3265 to 3280	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	3281 to 3296	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	3297 to 3312	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
15	3313 to 3328	0	0	0	0	0	0	0	0	0	0	224	255	0	0	0	0	0	0
	3329 to 3344	128	252	255	1	0	0	0	0	0	128	255	255	3	0	0	0	0	0
	3345 to 3360	224	255	255	7	0	0	0	0	0	252	255	255	7	0	0	0	0	0
	3361 to 3376	255	255	255	15	0	0	0	0	0	255	255	255	31	0	0	0	0	0
	3377 to 3392	255	255	255	31	0	0	0	0	0	255	255	255	63	0	0	0	0	0
20	3393 to 3408	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	3409 to 3424	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	3425 to 3440	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	3441 to 3456	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	3457 to 3472	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
25	3473 to 3488	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	3489 to 3504	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	3505 to 3520	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	3521 to 3536	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	3537 to 3552	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
30	3553 to 3568	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	3569 to 3584	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	3585 to 3600	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	3601 to 3616	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	3617 to 3632	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
35	3633 to 3648	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	3649 to 3664	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	3665 to 3680	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	3681 to 3696	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	3697 to 3712	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
40	3713 to 3728	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	3729 to 3744	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	3745 to 3760	0	0	0	0	0	0	0	0	0	0	0	96	0	0	0	0	0	0
	3761 to 3776	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	3777 to 3792	0	0	0	0	0	0	0	0	0	0	0	8	0	0	0	0	0	0
45	3793 to 3808	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	3809 to 3824	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	3825 to 3840	0	0	0	0	0	0	0	0	0	0	152	255	1	0	0	0	0	0
	3841 to 3856	0	241	255	1	0	0	0	0	0	0	254	255	3	0	0	0	0	0
	3857 to 3872	192	255	255	7	0	0	0	0	0	248	255	255	15	0	0	0	0	0
50	3873 to 3888	254	255	255	15	0	0	0	0	0	255	255	255	31	0	0	0	0	0
	3889 to 3904	255	255	255	63	0	0	0	0	0	255	255	255	63	0	0	0	0	0
	3905 to 3920	255	255	255	127	0	0	0	0	0	255	255	255	255	255	255	255	255	255
	3921 to 3936	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	3937 to 3952	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
55	3953 to 3968	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	3969 to 3984	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	3985 to 4000	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	4001 to 4016	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	4017 to 4032	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
60	4033 to 4048	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	4049 to 4064	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	4065 to 4080	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	4081 to 4096	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	4097 to 4112	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
65	4113 to 4128	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	4129 to 4144	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	4145 to 4160	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	4161 to 4176	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	4177 to 4192	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
70	4193 to 4208	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	4209 to 4224	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	4225 to 4240	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	4241 to 4256	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	4257 to 4272	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
75	4273 to 4288	0	0	4	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	4289 to 4304	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	4305 to 4320	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	4321 to 4336	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	4337 to 4352	0	0	0	0	0	0	0	0	0	0	96	255	1	0	0	0	0	0
80	4353 to 4368	0	192	255	3	0	0	0	0	0	0	248	255	7	0	0	0	0	0
	4369 to 4384	0	255	255	7	0	0	0	0	0	224	255	255	15	0	0	0	0	0
	4385 to 4400	252	255	255	31	0	0	0	0	0	255	255	255	31	0	0	0	0	0
	4401 to 4416	255	255	255	63	0	0	0	0</										

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	11185 to 11200	255	255	255	255	255	63	0	0	255	255	255	255	255	127	0	0
	11201 to 11216	255	255	255	255	255	127	0	0	255	255	255	255	255	255	255	0
	11217 to 11232	255	255	255	255	255	255	1	0	255	255	255	255	255	255	255	255
5	11233 to 11248	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	11249 to 11264	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	11265 to 11280	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11281 to 11296	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11297 to 11312	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
10	11313 to 11328	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11329 to 11344	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11345 to 11360	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11361 to 11376	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11377 to 11392	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
15	11393 to 11408	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11409 to 11424	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11425 to 11440	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11441 to 11456	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11457 to 11472	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
20	11473 to 11488	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11489 to 11504	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11505 to 11520	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11521 to 11536	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11537 to 11552	0	0	0	0	0	0	0	0	0	0	0	192	1	0	0	0
25	11553 to 11568	0	0	0	248	1	0	0	0	0	0	0	254	3	0	0	0
	11569 to 11584	0	0	192	255	7	0	0	0	0	0	248	255	15	0	0	0
	11585 to 11600	0	0	255	255	15	0	0	0	0	224	255	255	31	0	0	0
	11601 to 11616	0	252	255	255	63	0	0	0	0	255	255	255	127	0	0	0
30	11617 to 11632	224	255	255	255	127	0	0	0	252	255	255	255	255	0	0	0
	11633 to 11648	255	255	255	255	255	1	0	0	255	255	255	255	255	1	0	0
	11649 to 11664	255	255	255	255	255	3	0	0	255	255	255	255	255	7	0	0
	11665 to 11680	255	255	255	255	255	15	0	0	255	255	255	255	255	15	0	0
	11681 to 11696	255	255	255	255	255	31	0	0	255	255	255	255	255	63	0	0
	11697 to 11712	255	255	255	255	255	63	0	0	255	255	255	255	255	127	0	0
35	11713 to 11728	255	255	255	255	255	255	0	0	255	255	255	255	255	255	1	0
	11729 to 11744	255	255	255	255	255	255	1	0	255	255	255	255	255	255	3	0
	11745 to 11760	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	11761 to 11776	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
40	11777 to 11792	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11793 to 11808	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11809 to 11824	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11825 to 11840	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11841 to 11856	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11857 to 11872	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
45	11873 to 11888	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11889 to 11904	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11905 to 11920	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11921 to 11936	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11937 to 11952	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
50	11953 to 11968	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11969 to 11984	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	11985 to 12000	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12001 to 12016	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12017 to 12032	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
55	12033 to 12048	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0
	12049 to 12064	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12065 to 12080	0	0	0	224	3	0	0	0	0	0	0	252	7	0	0	0
	12081 to 12096	0	0	0	255	7	0	0	0	0	0	224	255	15	0	0	0
60	12097 to 12112	0	0	252	255	31	0	0	0	0	128	255	255	31	0	0	0
	12113 to 12128	0	240	255	255	63	0	0	0	0	254	255	255	127	0	0	0
	12129 to 12144	128	255	255	255	255	0	0	0	240	255	255	255	255	0	0	0
	12145 to 12160	254	255	255	255	255	1	0	0	255	255	255	255	255	3	0	0
	12161 to 12176	255	255	255	255	255	3	0	0	255	255	255	255	255	7	0	0
	12177 to 12192	255	255	255	255	255	15	0	0	255	255	255	255	255	31	0	0
65	12193 to 12208	255	255	255	255	255	31	0	0	255	255	255	255	255	63	0	0
	12209 to 12224	255	255	255	255	255	127	0	0	255	255	255	255	255	127	0	0
	12225 to 12240	255	255	255	255	255	255	0	0	255	255	255	255	255	255	1	0
	12241 to 12256	255	255	255	255	255	255	3	0	255	255	255	255	255	255	3	0
	12257 to 12272	255	255	255	255	255	255	7	0	255	255	255	255	255	255	15	0
70	12273 to 12288	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255
	12289 to 12304	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12305 to 12320	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12321 to 12336	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12337 to 12352	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
75	12353 to 12368	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12369 to 12384	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12385 to 12400	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12401 to 12416	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
80	12417 to 12432	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12433 to 12448	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12449 to 12464	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12465 to 12480	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12481 to 12496	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12497 to 12512	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
85	12513 to 12528	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12529 to 12544	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12545 to 12560	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12561 to 12576	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12577 to 12592	0	0	0	128	3	0	0	0	0	0	0	240	7	0	0	0
90	12593 to 12608	0	0	0	254	15	0	0	0	0	0	192	255	15	0	0	0
	12609 to 12624	0	0	240	255	31	0	0	0	0	0	254	255	63	0	0	0
	12625 to 12640	0	192	255	255	63	0	0	0	0	255	255	255	255	1	0	0
	12641 to 12656	0	255	255	255	255	0	0	0	192	255	255	255	255	3	0	0
	12657 to 12672	248	255	255	255	255	1	0	0	255	255	255	255	255	15	0	0
95	12673 to 12688	255	255	255	255	255	7	0	0	255	255	255	255	255	255	15	0

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5	12801 to 12816	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12817 to 12832	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12833 to 12848	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12849 to 12864	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12865 to 12880	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
10	12881 to 12896	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12897 to 12912	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12913 to 12928	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12929 to 12944	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12945 to 12960	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
15	12961 to 12976	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12977 to 12992	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	12993 to 13008	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13009 to 13024	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13025 to 13040	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
20	13041 to 13056	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13057 to 13072	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13073 to 13088	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13089 to 13104	0	0	0	0	6	0	0	0	0	0	0	192	7	0	0	0
	13105 to 13120	0	0	0	248	15	0	0	0	0	0	0	255	31	0	0	0
25	13121 to 13136	0	0	224	255	31	0	0	0	0	0	248	255	63	0	0	0
	13137 to 13152	0	0	255	255	127	0	0	0	0	224	255	255	255	0	0	0
	13153 to 13168	0	252	255	255	255	0	0	0	128	255	255	255	255	1	0	0
	13169 to 13184	224	255	255	255	255	3	0	0	252	255	255	255	255	3	0	0
	13185 to 13200	255	255	255	255	255	7	0	0	255	255	255	255	255	15	0	0
30	13201 to 13216	255	255	255	255	255	31	0	0	255	255	255	255	255	31	0	0
	13217 to 13232	255	255	255	255	255	63	0	0	255	255	255	255	255	127	0	0
	13233 to 13248	255	255	255	255	255	127	0	0	255	255	255	255	255	255	0	0
	13249 to 13264	255	255	255	255	255	255	1	0	255	255	255	255	255	255	3	0
	13265 to 13280	255	255	255	255	255	255	3	0	255	255	255	255	255	255	7	0
35	13281 to 13296	255	255	255	255	255	255	15	0	255	255	255	255	255	255	15	0
	13297 to 13312	255	255	255	255	255	255	31	0	255	255	255	255	255	255	63	0
	13313 to 13328	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13329 to 13344	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13345 to 13360	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
40	13361 to 13376	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13377 to 13392	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13393 to 13408	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13409 to 13424	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13425 to 13440	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
45	13441 to 13456	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13457 to 13472	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13473 to 13488	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13489 to 13504	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13505 to 13520	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
50	13521 to 13536	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13537 to 13552	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13553 to 13568	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13569 to 13584	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13585 to 13600	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
55	13601 to 13616	0	0	0	0	4	0	0	0	0	0	0	0	15	0	0	0
	13617 to 13632	0	0	0	224	15	0	0	0	0	0	0	252	31	0	0	0
	13633 to 13648	0	0	128	255	63	0	0	0	0	0	240	255	63	0	0	0
	13649 to 13664	0	0	252	255	127	0	0	0	128	255	255	255	255	0	0	0
	13665 to 13680	0	240	255	255	255	1	0	0	0	254	255	255	255	1	0	0
60	13681 to 13696	192	255	255	255	255	3	0	0	240	255	255	255	255	7	0	0
	13697 to 13712	254	255	255	255	255	7	0	0	255	255	255	255	255	15	0	0
	13713 to 13728	255	255	255	255	255	31	0	0	255	255	255	255	255	63	0	0
	13729 to 13744	255	255	255	255	255	63	0	0	255	255	255	255	255	127	0	0
	13745 to 13760	255	255	255	255	255	255	0	0	255	255	255	255	255	255	1	0
65	13761 to 13776	255	255	255	255	255	255	1	0	255	255	255	255	255	255	3	0
	13777 to 13792	255	255	255	255	255	255	7	0	255	255	255	255	255	255	7	0
	13793 to 13808	255	255	255	255	255	255	15	0	255	255	255	255	255	255	31	0
	13809 to 13824	255	255	255	255	255	255	63	0	255	255	255	255	255	255	63	0
	13825 to 13840	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
70	13841 to 13856	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13857 to 13872	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13873 to 13888	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13889 to 13904	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13905 to 13920	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
75	13921 to 13936	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13937 to 13952	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13953 to 13968	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13969 to 13984	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	13985 to 14000	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
80	14001 to 14016	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	14017 to 14032	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	14033 to 14048	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	14049 to 14064	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	14065 to 14080	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
85	14081 to 14096	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	14097 to 14112	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	14113 to 14128	0	0	0	0	0	0	0	0	0	0	0	0	14	0	0	0
	14129 to 14144	0	0	0	128	31	0	0	0	0	0	0	240	31	0	0	0
	14145 to 14160	0	0	0	254	63	0	0	0	0	0	192	255	127	0	0	0
90	14161 to 14176	0	0	248	255	255	0	0	0	0	248	255	255	255	0	0	0
	14177 to 14192	0	192	255	255	255	1	0	0	0	224	255	255	255	3	0	0
	14193 to 14208	0	255	255	255	255	3	0	0	255	255	255	255	255	7	0	0
	14209 to 14224	252	255	255	255	255	15	0	0	255	255	255	255	255			

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5	14417 to 14432	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	14433 to 14448	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	14449 to 14464	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	14465 to 14480	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	14481 to 14496	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
10	14497 to 14512	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	14513 to 14528	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	14529 to 14544	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	14545 to 14560	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	14561 to 14576	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
15	14577 to 14592	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	14593 to 14608	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	14609 to 14624	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	14625 to 14640	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8	0	0	0
	14641 to 14656	0	0	0	0	31	0	0	0	0	0	0	0	192	63	0	0	0	0
20	14657 to 14672	0	0	0	248	63	0	0	0	0	0	0	0	255	127	0	0	0	0
	14673 to 14688	0	0	224	255	255	0	0	0	0	0	252	255	255	1	0	0	0	0
	14689 to 14704	0	0	255	255	255	1	0	0	0	224	255	255	255	3	0	0	0	0
	14705 to 14720	0	252	255	255	255	7	0	0	128	255	255	255	255	7	0	0	0	0
	14721 to 14736	240	255	255	255	255	15	0	0	254	255	255	255	255	31	0	0	0	0
25	14737 to 14752	255	255	255	255	255	63	0	0	255	255	255	255	255	63	0	0	0	0
	14753 to 14768	255	255	255	255	255	127	0	0	255	255	255	255	255	255	0	0	0	0
	14769 to 14784	255	255	255	255	255	255	0	0	255	255	255	255	255	255	1	0	0	0
	14785 to 14800	255	255	255	255	255	255	3	0	255	255	255	255	255	255	7	0	0	0
	14801 to 14816	255	255	255	255	255	255	7	0	255	255	255	255	255	255	15	0	0	0
30	14817 to 14832	255	255	255	255	255	255	31	0	255	255	255	255	255	255	31	0	0	0
	14833 to 14848	255	255	255	255	255	255	63	0	255	255	255	255	255	255	127	0	0	0
	14849 to 14864	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	14865 to 14880	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	14881 to 14896	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
35	14897 to 14912	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	14913 to 14928	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	14929 to 14944	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	14945 to 14960	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	14961 to 14976	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
40	14977 to 14992	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	14993 to 15008	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	15009 to 15024	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	15025 to 15040	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	15041 to 15056	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
45	15057 to 15072	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	15073 to 15088	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	15089 to 15104	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	15105 to 15120	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	15121 to 15136	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
50	15137 to 15152	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	15153 to 15168	0	0	0	0	28	0	0	0	0	0	0	0	128	63	0	0	0	0
	15169 to 15184	0	0	0	224	127	0	0	0	0	0	0	0	252	255	0	0	0	0
	15185 to 15200	0	0	128	255	255	0	0	0	0	240	255	255	255	1	0	0	0	0
	15201 to 15216	0	0	254	255	255	3	0	0	0	192	255	255	255	3	0	0	0	0
55	15217 to 15232	0	240	255	255	255	7	0	0	0	254	255	255	255	15	0	0	0	0
	15233 to 15248	192	255	255	255	255	31	0	0	248	255	255	255	255	31	0	0	0	0
	15249 to 15264	255	255	255	255	255	63	0	0	255	255	255	255	255	127	0	0	0	0
	15265 to 15280	255	255	255	255	255	127	0	0	255	255	255	255	255	255	0	0	0	0
	15281 to 15296	255	255	255	255	255	255	1	0	255	255	255	255	255	255	3	0	0	0
60	15297 to 15312	255	255	255	255	255	255	3	0	255	255	255	255	255	255	7	0	0	0
	15313 to 15328	255	255	255	255	255	255	15	0	255	255	255	255	255	255	15	0	0	0
	15329 to 15344	255	255	255	255	255	255	31	0	255	255	255	255	255	255	63	0	0	0
	15345 to 15360	255	255	255	255	255	255	127	0	255	255	255	255	255	255	127	0	0	0
	15361 to 15376	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
65	15377 to 15392	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	15393 to 15408	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	15409 to 15424	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	15425 to 15440	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	15441 to 15456	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
70	15457 to 15472	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	15473 to 15488	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	15489 to 15504	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	15505 to 15520	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	15521 to 15536	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
75	15537 to 15552	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	15553 to 15568	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	15569 to 15584	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	15585 to 15600	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	15601 to 15616	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
80	15617 to 15632	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	15633 to 15648	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	15649 to 15664	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	15665 to 15680	0	0	0	0	48	0	0	0	0	0	0	0	0	62	0	0	0	0
	15681 to 15696	0	0	0	192	127	0	0	0	0	0	0	240	255	0	0	0	0	0
85	15697 to 15712	0	0	0	254	255	1	0	0	0	0	192	255	255	1				

	16033 to 16048		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	16049 to 16064		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	16065 to 16080		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
5	16081 to 16096		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	16097 to 16112		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	16113 to 16128		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	16129 to 16144		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	16145 to 16160		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
10	16161 to 16176		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	16177 to 16192		0	0	0	0	0	0	0	0	0	0	0	0	120	0	0	0
	16193 to 16208		0	0	0	0	127	0	0	0	0	0	0	224	255	0	0	0
	16209 to 16224		0	0	0	252	255	1	0	0	0	0	0	255	255	3	0	0
	16225 to 16240		0	0	224	255	255	3	0	0	0	0	252	255	255	7	0	0
15	16241 to 16256		0	128	255	255	255	15	0	0	0	240	255	255	255	15	0	0
	16257 to 16272		0	252	255	255	255	31	0	0	128	255	255	255	255	63	0	0
	16273 to 16288		240	255	255	255	255	127	0	0	254	255	255	255	255	127	0	0
	16289 to 16304		255	255	255	255	255	255	0	0	255	255	255	255	255	255	1	0
	16305 to 16320		255	255	255	255	255	255	3	0	255	255	255	255	255	255	3	0
	16321 to 16336		255	255	255	255	255	255	7	0	255	255	255	255	255	255	15	0
20	16337 to 16352		255	255	255	255	255	255	15	0	255	255	255	255	255	255	31	0
	16353 to 16368		255	255	255	255	255	255	63	0	255	255	255	255	255	255	127	0
	16369 to 16384		255	255	255	255	255	255	127	0	255	255	255	255	255	255	255	0

Step 603 begins the process of accessing the information when so arranged. More specifically, in step 603,

$$y_{(i,j)}^{(p,q)} = Y_{(i,j)}^{(p,q)} \gg 5$$

$$u_{(i,j)}^{(p,q)} = U_{(i,j)}^{(p,q)} \gg 2$$

and

$$v_{(i,j)}^{(p,q)} = V_{(i,j)}^{(p,q)} \gg 2$$

are calculated,

wherein, similar to that described hereinabove,

p points to the particular horizontal slice of the frame is being processed and q points to the particular column, or vertical slice, of the frame, i points to the particular row within the block that is being processed, j points to the particular column within the block that is being processed, and “ \gg ” is a right shift operation. Doing so leaves only the desired 8th to 3rd least significant bits of the pixels U value, the 8th to 3rd least significant bits of the pixels V value, and the 8th to 6th least significant bits of the pixels Y value. Thereafter, in step 605 the lookup table address for the current pixel is calculated as

as

$$LUT_Address_{(i,j)}^{(p,q)} = u_{(i,j)}^{(p,q)} \ll 9 + v_{(i,j)}^{(p,q)} \ll 3 + y_{(i,j)}^{(p,q)}, \text{ where “} \ll \text{” is a left-shift operation.}$$

Doing so combines the extracted bits into a combined address and points to the one byte that corresponds to the pixel. Thereafter, in step 607, the particular bit within the byte that corresponds to the pixel is determined, by using the value made up of the 2nd to 5th least significant bits of the Y component as an index into the byte. To this end, step 607 calculates

$$b = \text{mod}(Y_{(i,j)}^{(p,q)} \ll 2, 8)$$

where mod is the modulo function.

In step 609, the value of the b^{th} bit position of the byte at the calculated lookup table address is extracted, assigned as the value of a variable m , which is supplied as an output. Again, in this exemplary embodiment, if the extracted bit is a 1, U is the selected chrominance portion while if the extracted bit is a 0, V is the selected chrominance portion.

The process then exits in step 611.

Those of ordinary skill in the art will readily recognize how to adapt the foregoing to pixels in other formats, e.g., RGB or YIQ,

Note that if Huffman encoding of the table is desired, it may be advantageous that the foregoing correspondence of select U being a 1 and select V being a zero should be reversed, assuming, as has been seen experimentally, that U is selected for a majority of pixel combinations.

FIG. 8 shows another exemplary process by which the particular chrominance portion is selected to contain the watermarking information for a pixel, in accordance with the principles of the invention. The process is entered in step 801 when it is necessary to select a chrominance portion suitable to contain watermarking information. As in FIG. 6, for purposes of discussion of FIG. 8, it is assumed that the pixel is represented in YUV format. Furthermore, it is noted that, preferably, for each original 2x2 luminance block of original video, had the original video been in 4-4-4 representation, there should only one Y value for each chrominance component, i.e., each pair of respective corresponding U and V values. To this end, the Y values of the original block may be downsampled so as to have the same resolution as the U and V. Alternatively, the average, or some other combination, of the Y values associated with a particular U and V values may be computed and used as the Y value for the process of FIG. 8.

In order to further reduce the storage requirements in the embodiment of FIG. 8, as compared to the embodiment of FIG. 6, in accordance with an aspect of the invention, not only is the YUV colorspace divided into regions, each region including positions corresponding to at least one set of Y, U, and V values, with each region being assigned a chrominance portion, e.g., based on experimental observations, that is to be selected for any pixel whose Y, U, and V values fall within the region, as described in connection with FIG. 6, but any pixel that has a U value less than a predefined value, e.g., one-half the maximum value, has the U chrominance portion selected for watermarking. Thus, for 8 bit Y, U, and V, values, if the value of U is less than 128, the U chrominance portion is always selected for watermarking regardless of the values of V or Y. This is because human visual system is less sensitive to the blue component U than the V component.

In accordance with an aspect of the invention, by having the most significant address bits of the chrominance portion selection table correspond to the U-value-derived bits of the address, advantageously, the size of the table can be reduced by up to one half. This is achieved by adding a test to determine if the U value is less than one half the maximum value prior to forming the table address, and if the test result is YES, simply indicating to select the U chrominance portion and skipping the rest of the process of accessing the table, and also by subtracting one half the maximum U value from the actual U value prior to calculating the U-value-derived bits of the address. Thus, the section of the table employed for FIG. 6 corresponding to the most significant U bit being 0 is eliminated, and only that portion of the table where the most significant U bit is 1 is retained. However, the indexing into the remaining portion of the table is shifted by the subtraction from the U value of the one half of the maximum U value prior to forming the U-value-derived bits.

Thus, the table is arranged to be addressed using an address that has the most significant bits corresponding to the U values, the next least significant values corresponding to the V values and the least significant values corresponding to the Y values. In other words, the address of the bytes may be formed as follows:

$$U6|U5|U4|U3|U2|V7|V6|V5|V4|V3|V2|Y7|Y6|Y5$$

where U6,U5,U4,U3, and U2 are the values of the 7th to 3rd least significant bits of the pixels U value, V7,V6,V5,V4,V3, and V2 are the values of the 8th to 3rd least significant bits of the pixels V value, and Y7, Y6, and Y5, are the values of the 8th to 6th least significant bits of the pixels Y value. Then, the particular bit within the byte is specified by using the 5th to 2nd least significant bits of the Y component, e.g., Y4, Y3, and Y2.

To this end, conditional branch point 802 tests to determine if $U_{(i,j)}^{(p,q)} < predefined_value$, where *predefined_value* is, for example, one half the maximum U value. Note that to save a bit, and half the table size, preferably *predefined_value* should be a power of 2. If the test result in step 802 is NO, indicating that the value of U is less than the predefined value, e.g., one half the maximum value of U, e.g., 128, and hence the chrominance portion to be selected will be a function of Y, U, and V, and so the table must be accessed, control passes to step 803 to begin the process of accessing the table. In step 803,

$$y_{(i,j)}^{(p,q)} = Y_{(i,j)}^{(p,q)} \gg 5$$

$$u_{(i,j)}^{(p,q)} = (U_{(i,j)}^{(p,q)} - predefined_value) \gg 2, \text{ e.g., } u_{(i,j)}^{(p,q)} = (U_{(i,j)}^{(p,q)} - 128) \gg 2$$

and

$$v_{(i,j)}^{(p,q)} = V_{(i,j)}^{(p,q)} \gg 2$$

are calculated,

where, similar to that described hereinabove,

where p points to the particular horizontal slice of the frame is being processed
 5 and q points to the particular column, or vertical slice, of the frame, i points to the
 particular row within the block that is being processed, j points to the particular column
 within the block that is being processed, and “ \gg ” is a right-shift operation. Doing so
 leaves only the desired 7th to 3rd least significant bits of the pixels U value, the 8th to 3rd
 least significant bits of the pixels V value, and the 8th to 6th least significant bits of the
 10 pixels Y value. Thereafter, in step 805 the lookup table address for the current pixel is
 calculated as

$LUT_Address_{(i,j)}^{(p,q)} = u_{(i,j)}^{(p,q)} \ll 9 + v_{(i,j)}^{(p,q)} \ll 3 + y_{(i,j)}^{(p,q)}$, where “ \ll ” is a left-
 shift operation.

Doing so combines the extracted bits into a combined address and points to the
 15 one byte that corresponds to the pixel. Thereafter, in step 807, the particular bit within
 the byte that corresponds to the pixel is determined, by using the value made up of the 5th
 to 2nd least significant bits of the Y component as an index into the byte. To this end, step
 807 calculates

$$b = \text{mod}(Y_{(i,j)}^{(p,q)} \ll 2, 8)$$

20 where mod is the modulo function.

In step 809, the value of the b^{th} bit position of the byte at the calculated lookup
 table address is extracted and stored in the variable m . The value of variable m
 is supplied as an output in step 811. Again, if the output bit is a 1, U is the selected
 chrominance portion while if the extracted bit is a 0, V is the selected chrominance
 25 portion. The process then exits in step 813.

If the test result in step 802 is YES, indicating that the U chrominance portion
 should be selected, because the pixel color is not primarily blue and hence changing the
 blue color of the pixel will not be detected by the human visual system, control passes to
 step 815, in which the variable m is set equal to 1. Doing so assures that U is selected.
 30 Control then passes to step 811, and the process continues as described above.

Notwithstanding the foregoing improvements in color selection, with certain Y,
 U, and V values for a pixel, there is still, disadvantageously, a possibility that a slightly
 detectable flickering be manifest. This is because in order to survive MPEG-like
 encoding there may be a need to add large values to the average value of the selected
 35 chrominance portion.

FIG. 9 shows an exemplary transmitter arranged in accordance with the principles of the invention, and in which the flickering may be reduced by replicating the data to be impressed, at least once, and preferably two or more times, prior to its being impressed upon the average value of a chrominance portion of a block. The original and each
5 replica are transmitted in the same block position of separate consecutive frames. Preferably, the frames having like-positioned blocks carrying the same data are consecutive in display order. Furthermore, specific blocks of the frame may be embedded with a particular known data sequence, e.g., a Barker sequence, rather than encoded user data.

10 The embodiment of the invention in FIG. 9 is similar to that of FIG. 1. All like-numbered elements of FIG. 9 operate substantially the same as in FIG. 1. In addition to those elements of FIG. 1 that are shown in FIG. 9 are repeater 925 and optional sequence adder 927. In addition, bit mapper 123 of FIG. 1 is optionally replaced in FIG. 9 by bit mapper 923. Replacement of bit mapper 123 by bit mapper 923 is necessary only
15 if the additional functionality described hereinbelow in connection with bit mapper 923 is desired.

Repeater 925 receives bits either from block interleaver 121 or optional sequence adder 927. Repeater 925 stores the received bits and outputs them for like-positioned blocks of at least two frames. In one embodiment of the invention, it has been found that
20 good results are achieved when repeater 925 stores the received bits and outputs them for the like-positioned blocks of three frames. Those of ordinary skill in the art will be able to trade-off any perceived flicker with desired throughput of the watermark data by choosing the number frames for which the data is repeated.

Optional sequence adder 927 embeds a particular known data sequence, e.g., a
25 Barker sequence, in specific blocks of the frame, the data sequence being in lieu of encoded user data. The specific blocks in which the data sequence is encoded may be scattered throughout the blocks of a frame. Each group of initial and repeated data frames may employ a different known sequence. Doing so will enable the receiver to detect the grouping of the frames. Alternatively, the same sequence may be employed for each
30 group but the specific blocks used for the sequence may be different for consecutive groups.

FIG. 10 shows an exemplary embodiment of a receiver arranged in accordance with the principles of the invention for use in receiving a watermarked video signal, such as that produced by the transmitter of FIG. 9. The embodiment of the invention in FIG.
35 10 is similar to that of FIG. 2. All like-numbered elements of FIG. 10 operate substantially the same as they do in FIG. 2. In addition to those elements of FIG. 2 there

are shown in FIG. 10 sequence processor 1025 and frame weighting unit 1027. Furthermore, channel decoder 221 of FIG. 2 is optionally replaced in FIG. 10 by channel decoder 1021.

A receiver, e.g., as shown in FIG. 10, may detect group synchronization using
5 sequence processor 1025. This may be performed by adding up the values of the group
identification sequence from each frame of a group-length-number of consecutive frames,
which thus are employed as a synchronization pattern, and determining if the result
exceeds a prescribed threshold. If the threshold is exceeded, it is assumed that the first
10 frame whose expected synchronization pattern value was added is the first frame in the
group. If the threshold is not exceeded, it is assumed that the first frame whose value was
added is not the first frame of a group. This is analogous to performing an
autocorrelation on the synchronization pattern. Those of ordinary skill in the art will
recognize that other conventional techniques for avoiding false matches, as well as
15 handling missing the first frame due to errors, such as searching for a maximum prior to
declaring group synchronization, may be employed.

Advantageously, once the receiver detects the regular group pattern, any time
there is a deviation from the pattern the receiver will be able to recognize that a frame of
the original video sequence has been removed. Such information may be supplied as an
output by sequence processor 1025.

20 For example, various commercials of a vendor within a video signal may be
monitored. The vendor may be assigned a unique code that is embedded in each frame of
its commercial. A receiver is made aware of the particular unique code and which blocks
of the watermarked frames should contain the code. By detecting the appearance of the
code within watermarked frames, the receiver can identify a frame as being one that
25 belongs to one of the commercials of the vendor. Once a frame with the code is detected,
the number of sequential frames incorporating the code can be counted to determine the
length of the commercial. If the number of frames counted is less than the anticipated
number of frames based on the known length of the commercial when it was originally
watermarked, it may be assumed that the commercial was inappropriately shortened by
30 removing the number of frames that corresponds to the difference between the anticipated
number of frames and the counted number of frames. Those of ordinary skill in the art
will recognize that other conventional techniques for avoiding false matches, as well as
handling missing the first frame due to errors, may be employed.

Each frame of the commercial, or groups of frames within the commercial, may
35 be watermarked with a unique identifier, e.g., a frame or group number, which is part of a
distinct sequence over the frame. When a gap in the expected sequence is detected due to

one or more missing frames, the missing frames may be specifically identified when each frame has a unique identifier. When identifiers are assigned only to groups and the number of frames in each group is known, only the particular group to which any missing frames belongs may be identified, along with the count of how many frames are missing.

5 Although replication of the data may be employed to reduce flicker, as indicated hereinabove, doing so may limit the ability to detect missing frames to merely identifying the group from which the frame is missing, rather than being able to identify the particular frame. Therefore, although the watermark data is generally replicated, at least an individual frame identifier may not be replicated. The blocks containing such non-
10 replicated frames are placed where they will be least likely to attract attention should they cause flickering, e.g., the corners of the frame. Doing so provides the majority of the benefit of reducing detectable flicker, while also allowing particular individual frames that are missing to be detected.

 If a vendor has different commercials, each of the commercials may have a further
15 sequence embedded in at least one of its frames to identify the particular commercial of that vendor that is being received.

 Should multiple vendors have watermarked commercials, so long as each vendor is assigned a unique code, a system monitoring for the appearance of the commercials of a first vendor with a first unique code will ignore commercials of a second vendor with a
20 second unique code. Alternatively, a single system may monitor a video signal for the appearance of commercials from different vendors that each have a unique code, and the results may be segregated by vendor based on their codes.

 In another arrangement in which multiple vendors have watermarked commercials, each vendor employs the same code, and the code may even be at the same
25 block locations within the frame for each vendor. However, all the subsequent data contained within the frame is encrypted using a unique key for each vendor and each vendor has a receiver that knows only the key for that vendor. Therefore, each vendor can only decrypt and receive data from its own commercials. In another arrangement, the data for each vendor may be encrypted by scrambling the data over the blocks of a frame.
30 Each receiver would know only the scrambling pattern for its associated vendor.

 Monitoring for an initial appearance of a code indicating the start of a commercial may be performed continuously, or within a window of time during which the commercial is expected to be broadcast.

 In accordance with an aspect of the invention, instead of simply repeating the data
35 over the multiple frames of a group and then using bit mapper 123 (FIG. 1), the amount added to the average value of a chrominance portion of a block, which depends on the

complexity of the block and its anticipated quantization level, may be changed slightly from frame to frame over a group, even when the complexity of the block is the same at corresponding locations from frame to frame. The change that is made is small with respect to the value being added to the average to place the watermark bit within the average value. Such changes may be performed by bit mapper 923 (FIG. 9), thereby providing additional coding gain that may be advantageously employed to improve the reliability of the data at the receiver. However, doing so may cause a slight reduction in visual quality of low texture areas, because a few pixels within the block may have different values than their predecessors in the same location. However, because such reduction is at the pixel level, it is typically not noticeable.

In one arrangement, groups of three time-consecutive frames are transmitted with the same watermark data being impressed thereon. The middle frame of the group is watermarked as described above in connection with FIG. 3, without changing the amount added to the average value of the selected chrominance portion of the block from the value determined in FIG. 3.

The first-in-time frame of the group also has a value computed to be added, i.e., an offset bias, by bit mapper 923 (FIG. 9), to the average value of the selected chrominance portion of the block that is developed as described in connection with FIG. 3. However, the bias, e.g., one quarter or, preferably one half, of the absolute value of the value being added to the average to place the watermark bit within the average value, is additionally added to the computed average value of the chrominance portion selected to carry the watermark data. Thus, for example, if one is being added to the average value to place the watermark bit within the average value, then one half is added to the average value. This translates to adding 32 to the sum of the values of the selected chrominance portion of all the pixels of the block when there are 64 pixels in a block. Thus, summer 133 will received a higher value than it would have had the bias not been added. Similarly, as another example, if -4 is being added to the average value to place the watermark bit within the average value, if one half of the absolute value of the value added to the average value is employed, this translates to adding 128 to the sum of the values of the selected chrominance portion of all the pixels of the block when there are 64 pixels in a block.

Note that this additional bias amount, e.g., 32, will be distributed throughout the various pixels based on their luminance variances. Also, this addition of the bias is independent of any value added to the average to bring it with a safe range. As a result, the average value may fall outside of the safe range. However, the increase in error

probability engendered by moving out of the safe range is more than offset by the resulting coding gain resulting from employing the bias.

The last-in-time frame of the group has a value computed to be subtracted, i.e., an offset bias, by bit mapper 923 (FIG. 9), from the average value of the selected chrominance portion of the block that is developed as described in connection with FIG. 3. However, the bias, e.g., one quarter or, preferably one half, of the absolute value of the value being added to the average to place the watermark bit within the average value, is additionally subtracted from the computed average value of the chrominance portion selected to carry the watermark data. Thus, for example, if -3 is being added to the average value to place the watermark bit within the average value, then one half of the absolute value of -3, i.e., 1.5, is subtracted from the average value. This translates to subtracting 96 from the sum of the values of the selected chrominance portion of all the pixels of the block when there are 64 pixels in a block. Thus, summer 133 will received a lower value than it would have had the bias not been subtracted. Similarly, as another example, if 2 is being added to the average value to place the watermark bit within the average value, then one half of the absolute value of 2, i.e., 1, is subtracted from the average value. This translates to subtracting 64 from the sum of the values of the selected chrominance portion of all the pixels of the block when there are 64 pixels in a block.

Note that the loss of the subtracted bias amount, e.g., 32, will be distributed throughout the various pixels based on their luminance variances. Further note that this subtraction of bias is independent of any value added to the average to bring it with a safe range. As a result, the average value may fall outside of the safe range. However, the increase in error probability engendered by moving out of the safe range is more than offset by the resulting coding gain.

One way to think about how this works is to look at FIG. 5. As described hereinabove, without considering the bias amount oftentimes just enough is added to, or subtracted from, the average value of the selected chrominance portion of a block in order to reach one of the outer borders of the safe range. Thus, prior to any bias, many frames are on or near the border of the safe range. The middle frame to which nothing is added or subtracted remains right on the border. The frame to which a slight bias is added may move slightly to be better positioned within the safe range, or it may move slightly out of the safe range. The frame from which a slight bias is subtracted moves in the opposite direction as the frame to which the bias is added. Thus, in the worst case, for a group of three frames one will be within the safe range, one will be on the border of the safe range, and one will be slightly out of the safe range. This results in an independent spread of values.

The effect of the bias may be further magnified because of the quantization that is performed by MPEG-like encoding and the separate MPEG-bias that is added during the MPEG dequantization. This can result in significant differences in the received data values for like-positioned blocks within consecutive frames even when the same bit is transmitted over those consecutive frames.

At the receiver, e.g., as shown in FIG. 10, the data extracted from each frame is weighted appropriately using maximum ratio combining based on a quality level that is believed to be present for each frame, e.g., in frame weighting unit 1027. To this end, sequence processor 1025 may supply to frame weighting unit 1027 a) frame synchronization information, so that frame weighting 1027 can know which frames are grouped together, and b) the number of errors in the synchronization pattern of each frame. The quality level is determined based on how many errors are believed to be in the received frame, which can be determined based on how many errors there are in the synchronization pattern that is expected for that frame, as extracted by sequence processor 1025. Table 1 shows a number of errors for each synchronization pattern and a respective weight that has been empirically derived to be appropriate for a frame with such a number of errors in its synchronization pattern. In other words, the values of the extracted data from each frame may be treated as soft data that is weighted by its associated weight as part of the combining process.

Based on the weights, the multiple instances of the same data bit for corresponding block locations in successive frames are extracted and combined to form a single received bit. This may be achieved by computing

$$bit_out = (2^n - 1) \frac{w_1 bit_1 + w_2 bit_2 + w_3 bit_3}{(w_1 + w_2 + w_3)}, \text{ where}$$

bit_out is the final output bit for the group of three frames;

w_1 , w_2 , and w_3 are the weights for each of the first, second and third in time frames;

bit_1 , bit_2 , and bit_3 are the bits from the like-positioned block of the first, second and third in time frames; and

n is the number of bits that the soft decoder input precision.

To best make use of the soft information, channel decoder 1021 is a so-called soft decoder that employs soft data bits, i.e., data bits that are each represented as a non binary number the range of which depends on the soft decoder input precision. For example, an 8 bit input precision soft decoder operates with values between 0 and 255. To this end the weighted average of the received hard bits, $\frac{w_1 bit_1 + w_2 bit_2 + w_3 bit_3}{(w_1 + w_2 + w_3)}$, is multiplied by

$2^n - 1$, thereby converting the weighted average into a soft value of the appropriate precision that can be processed by the soft decoder.

When the determined quality of a particular frame is below a prescribed threshold, it may be assumed that the particular frame does not contain any watermarking data and no data is extracted for that frame.

Those of ordinary skill in the art will readily recognize that which frame has the value added, which has it subtracted and which has no change; whether addition and subtraction are both necessary; the number of frames in a group; and any rounding to be performed on the value to be added or subtracted or the resulting value are at the discretion of the implementer.

Number of synchronization bit errors	Weight factor w
0	1
1	0.9
2	0.8
3	0.7
4	0.6
5	0.5
6	0.4